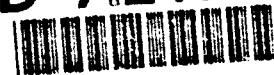


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A COMPUTER SOLUTION FOR MULTIPLE SATELLITE-SATELLITE AND  
SATELLITE-GROUND STATION VISIBILITY DETERMINATION

prepared by:

2Lt Jennifer L. Moore  
UTSI  
31 July 1991

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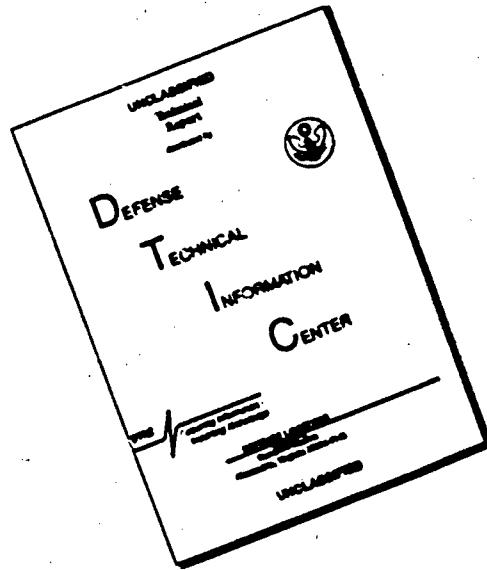
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## ABSTRACT

The purpose of this study is to examine the problem of determining rise and set times for visibility periods of multiple satellite/satellite and satellite-ground station communications. Additionally, the ability to maintain constant communication links is explored.

This research examines three means to solve the problem: basic iteration, the Lawton Method, and an improved method involving parabolic blending and a closed form root solving technique. The greatest concentration is placed on the final solution and its application.

The result of this investigation is a computer program capable of determining rise and set times for as many as four satellites and four ground stations. In addition, the program performs a check for continuous communications between the indicated satellites and earth based resources.

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## ACKNOWLEDGMENTS

This study represents the continued efforts of a project I began in a senior research study at the United States Air Force Academy. My task there was to research a computer method for rise/set determination between only two satellites using parabolic blending. My involvement with the project ended with the research, development, and early data collection. Two officers from the Academy, Lt Colonel Salvator Alfano and Captain Dave Negron continued their own research into this topic after my graduation and have since submitted the results of our total effort for publication (See reference 1).

For this project, I resumed my work where my own research had ended a year before. The data published from Lt Colonel Alfano and Captain Negron's continued efforts was very helpful in verifying the results of my own computer program. I am pleased to be able to bring to this project the added dimension of multiple satellite and ground station handling and continuous communications determination. I hope this paper provides insight into my own understanding of the problem and the course of my research as a whole. I am grateful to Lt Colonel Alfano and Captain Negron for their continued support and encouragement in this endeavor.

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## LIST OF SYMBOLS AND ABBREVIATIONS

a	Semi-major axis
$a_e$	Radius of the earth
$C_{max}$	Greatest modulus of the FFT
e	Eccentricity
$e_e$	Eccentricity of the earth
E	Eccentric anomaly
FFT	Fast Fourier Transform
i	Inclination
H	Altitude above mean sea level
$J_2$	Second harmonic of the earth's gravitational potential
JD	Julian Date
L	Geodetic Latitude
M	Mean anomaly
n	Mean motion
$n_0$	Mean motion at epoch
$n_a$	Anomalistic mean motion
p	Semi-latus rectum
P	Period of the visibility waveform
R <sub>E</sub>	Radius of the earth
r <sub>1</sub>	Position vector of satellite =1
r <sub>2</sub>	Position vector of satellite =2
T <sub>u</sub>	Centuries until 1 January 2000
UT	Universal Time
$\alpha_1$	Angle between earth's radius (perpendicular to tangent plane) and position vector =1, r <sub>1</sub>

$\alpha_2$	Angle between earth's radius (perpendicular to tangent plane) and position vector #2, $r_2$
$a_0, \dots, a_3$	Coefficients of the cubic equation defined by parabolic blending
$\Gamma$	Visibility function
$S$	East Longitude of the site
$\theta$	Local Sidereal Time
$\theta_g$	Greenwich Sidereal Time
$\theta_{go}$	Greenwich Sidereal Time at 0 hours UT
$\Phi$	Angle between $r_1$ and $r_2$
$v$	True anomaly
$\Omega$	Longitude of the ascending node
$w$	Argument of periapsis
$V_{max}$	Frequency of the largest modulus $C_{jmax}$

## CHAPTER 1

### INTRODUCTION

In space mission architecture, much rests on a satellite's ability to communicate with either an earth based tracking station or another satellite. Data relays as well as tracking, telemetry, and command directions depend on line of sight opportunities. Additionally, availability of communications determine satellite data rate requirements, data storage capabilities, and on orbit processing. All these factors affect satellite complexity, orbit selection and satellite constellation size. For these reasons, it is important to possess the ability to rapidly determine visibility rise and set times.

Three methods of determining the desired rise and set times are of interest to this study. The first propagates a basic visibility function then requires linear interpolation to find rise/set times. The second takes advantage of the fast Fourier transform to define characteristics of the visibility curve. This method makes use of the Regula Falsi iterative technique to determine rise/set times. The final method reconstructs the visibility curve using parabolic blending, then determines rise/set times using a closed form root solver. The process for determining visibility periods by this third method is detailed. The final result is a computer program capable of handling multiple satellites and ground stations, determining whether or not continuous

communications among the satellites and with the ground is possible, and completing the task in a timely manner.

## CHAPTER 2

### VISIBILITY FUNCTION

#### 2.1 General Discussion

The concept of the visibility function is central to any method of determining rise/set times for satellite-satellite or satellite-ground station in-view periods. The visibility function involves a line of sight calculation between the two objects of interest. The value of the function varies with time in accordance to the changing positions of the two objects.

For two satellites in orbit around the earth, line of sight is possible only when both objects are above a plane tangent to the earth's surface. The most extreme positions for the satellites which still allow for line of sight occur when both lie in the tangent plane. These positions are defined by the following equations<sup>6</sup>:

$$\alpha_1 = \cos^{-1}(R_1/r_1)$$

$$\alpha_2 = \cos^{-1}(R_2/r_2)$$

The angle between the two position vectors at any point is defined as:

$$\phi = \frac{\langle r_1 \cdot r_2 \rangle}{\|r_1\|\|r_2\|}$$

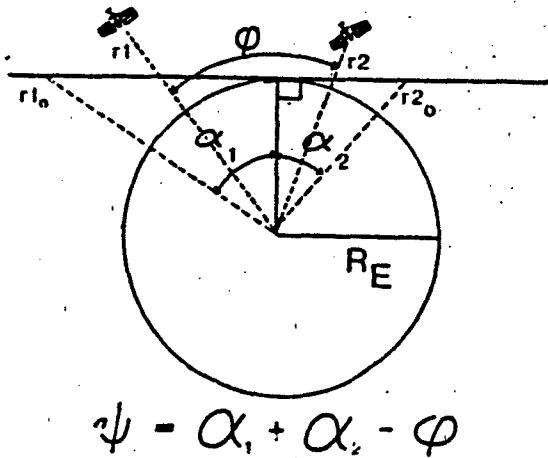
The visibility function is then defined by<sup>6</sup>:

$$\Gamma = \alpha_1 + \alpha_2 - \phi$$

When the value of the visibility function is positive, the satellites have line of sight. Similarly, a negative value indicates no line of sight. A value of zero is either a

rise or set time for visibility (See Figure 1). The same visibility function applies to a satellite and a ground station.

### Orbital Geometry



$$\psi = \alpha_1 + \alpha_2 - \phi$$

Figure 1

### 2.2 Basic Rise\Set Determination

The most direct method of determining visibility opportunities is small time step progression of the visibility function. At each step, the value of the visibility function is calculated. When plotted versus time, the visibility function yields a visibility waveform. When a sign change occurs in the value of the function and the wave crosses the x axis, a rise or set time is indicated. Linear interpolation is used to determine the exact time of the crossing. Although this method is legitimate, it is cumbersome and time consuming. The small time step necessary to insure the best solutions using

linear interpolation leads to large data sets and an extremely inefficient number of calculations by the computer. In order to determine the rise/set time for two satellite over a period of twenty-four hours with a time step of five seconds, more than seventeen-thousand calculations of the visibility function alone must be computed. As a method for real time solutions, this process is simply not realistic.

## CHAPTER 3

### THE LAWTON METHOD

#### 3.1 The Fast Fourier Transform

In his paper, J. A. Lawton presents a method for determining visibility opportunities using a fast Fourier transform, FFT, to estimate the period of the visibility waveform<sup>5</sup>. The use of the FFT is in response to the need to process large quantities of data points with fewer calculations while still maintaining the accuracy of the interpolating trigonometric polynomial<sup>4</sup>. In his presentation, Lawton uses the FFT to select the most prominent modulus of the waveform from the equation<sup>6</sup>

$$C_j = \sum_{k=1}^n F(t_k) e^{-j2\pi j k/n} \quad j = 1, 2, \dots, n$$

where

$F(t_k)$  = the visibility function at time  $t_k$

$i = \sqrt{-1}$

$n$  = number of data points

The value of  $C_j$  with the largest modulus,  $C_{jmax}$ , is then used to determine the value of the period of the waveform from the following equations<sup>6</sup>.

$$\omega_{jmax} = \frac{2\pi(j_{max} - 1)}{n}$$

$$P = \frac{2\pi}{\omega_{jmax}}$$

Once the period of the waveform is determined, it is used in conjunction with a curve searching technique to determine the rise/set times of the objects in question.

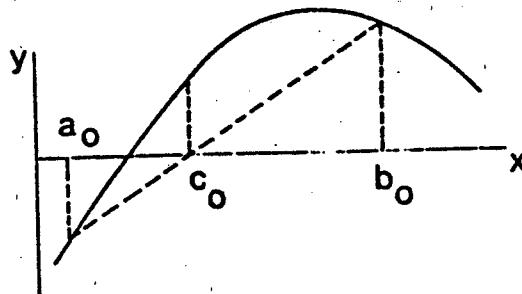
### 3.2 The Regula-Falsi Method of Zero Finding

The visibility waveform is first sectioned by fractions of the period determined by the FFT. The slope of the visibility function is determined in each progressive section of the wave until a local maximum value of the function is isolated between a positive and negative slope value. If the local maximum value is found to be positive, indicating line of sight is possible, then the portion of the curve in that particular section is searched for rise and set times. If the value of the visibility function is negative at the local maximum, the searching process resumes to isolate the next local maximum value<sup>s</sup>.

Curve searching in this process is accomplished using the Regula Falsi method of zero finding. The equations is<sup>7</sup>:

$$c_0 = \frac{a_0 f(b_0) - b_0 f(a_0)}{f(b_0) - f(a_0)}$$

An illustration of the process is shown below in Figure 2.



$$c_0 = \frac{a_0 f(b_0) - b_0 f(a_0)}{f(b_0) - f(a_0)}$$

Figure 2

If the value of  $f(c_0)$  is zero, the search is complete. Otherwise, an iterative technique begins with reassignment of the variables occurring as follows<sup>7</sup>:

if  $f(a_0)f(c_0) < 0$ , then  $a_1 = a_0$  and  $b_1 = c_0$   
if  $f(a_0)f(c_0) > 0$ , then  $a_1 = c_0$  and  $b_1 = b_0$

The above reassignment continues and the value of  $c$  is recalculated until  $f(c_0)$  is equal to zero. In the initial process of the curve examination, this method is used to determine the time associated with a local maximum in order to determine if the value of the visibility function at the local maximum is positive or negative. In this case, no crossing of the  $x$  axis takes place and the iteration of the Regula Falsi method continues until  $a_0 = b_0$  or until the difference between  $a_0$  and  $b_0$  is sufficiently small.

Although the Lawton process is sound in the determination of rise/set times, it has the disadvantage of being limited to orbits with eccentricities less than  $0.10^{\circ}$ . This is necessary to ensure a relatively periodic waveform. Very low eccentricity or nearly circular orbits produce nearly sinusoidal waves while highly elliptical orbits produce wave forms much more difficult to predict. Evidence of this can be found in the figures included with the results to this work. Aperiodic waveforms may result in inaccurate determination of the period and make curve searching a more difficult task. Additionally, this method is only applicable to evenly spaced data points<sup>4</sup>. Sparse data or unevenly spaced points cannot be used with the fast Fourier transform.

In his work, Lawton states this method accounted for 99.997% of the rise/set times determined by the iteration method described previously using a spherical-Earth gravity field and 99.992% of the rise/set times in an oblate-Earth gravity field.<sup>5</sup> He fails to state the accuracy of the rise/set times found by this method as compared to the basic iteration technique. The work in this study did not include reproduction of his results nor investigation of the accuracy of this method.

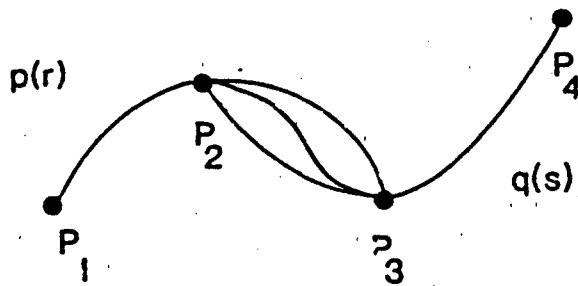
## CHAPTER 4

### THE PARABOLIC BLENDING TECHNIQUE

Parabolic blending is a method of curve fitting which maintains continuity of two parabolas formed from four data points. The first parabola,  $p(r)$  is defined by points 1, 2 and 3, while the second,  $q(s)$  includes points 2, 3, and 4. The parabolically blended curve is formed between points 2 and 3 (See Figure 3) and is defined by<sup>9</sup>

$$C(t) = (1 - t)p(r) + tq(s)$$

where  $0 \leq t \leq 1$



$$C(t) = (1 - t)p(r) + tq(s)$$

Figure 3

At  $t = 0$ ,  $C(t)$  has the same slope as  $p(r)$  while at  $t = 1$ ,  $q(s)$  is the influential curve. The final result of the blending is a cubic maintaining characteristics of both

parabolas. The equation of the curve is written as<sup>1,9</sup>

$$C(t) = a_3 t^3 + a_2 t^2 + a_1 t + a_0$$

where  $a_0 = P_2$

$$a_1 = -.5P_1 + .5P_3$$

$$a_2 = P_1 - 2.5P_2 + 2P_3 - .5P_4$$

$$a_3 = -.5P_1 + 1.5P_2 - 1.5P_3 + .5P_4$$

This technique differs from the cubic spline since the equation of the blended curve is independent of all other data points except for the four points used to define the two parabolas<sup>9</sup>. Also, parabolic blending works well with both equally and unequally space data points<sup>1</sup>.

## CHAPTER 5

### FINAL ALGORITHM

The final result of this study is a computer program designed to give the user the option of determining the visibility opportunities between a combination of up to four satellites and four ground stations. More than four satellites or ground stations requires significantly more calculations and data storage. The step-by-step process of rise/set determination is detailed in the sections which follow.

#### 5.1 Satellite Position Determination

To begin the process of determining the rise/set times for satellite-satellite or satellite-ground station visibility, it is necessary to calculate the position vector of the satellite at the start of the time of interest. This requires that six critical orbital elements be known for this calculation. They are the mean motion ( $n$ ), inclination ( $i$ ), eccentricity ( $e$ ), longitude of the ascending node ( $\Omega$ ), argument of periapsis ( $w$ ), and the mean anomaly ( $M$ ). Although the position vector can be determined from a variety of elements, these six were chosen since they are readily known from an ephemeris of satellite information. These elements and the position of the satellite are determined with respect to the geocentric reference frame.

The first step in the determination of the position vector is the calculation of the eccentric anomaly. This is

completed through the use of the Newton-Raphson Iteration.

The equations are<sup>2</sup>:

$$M_n = E_n - e \sin(E_n)$$

$$E_{n+1} = E_n + \frac{M_n - M_n}{1 - e \cos(E_n)}$$

For the first iteration,  $M$  is used in the place of  $E_n$ . When  $E_{n+1}$  is calculated, a comparison is made between  $E_n$  and  $E_{n+1}$ . When the difference is sufficiently small, the iteration is stopped. For the final computer program, the tolerance was set for a difference less than 0.000001. Convergence of the iteration may be of concern for orbits with eccentricities approaching 1.0<sup>2</sup>. Once determined, the final value of  $E_n$  is used in the calculation of the true anomaly as follows<sup>2</sup>:

$$\cos(v) = \frac{e - \cos(E)}{e \cos(E) - 1}$$

$$\sin(v) = \frac{a(1 - e^2)}{p} \cdot \sin(E)$$

$$p = a(1 - e\cos(E))$$

Once the proper quadrant of  $v$  is determined, the position vector is calculated in the PQW or perifocal reference frame<sup>2</sup>.

$$r = r\cos(v)P + r\sin(v)Q$$

$$r = \frac{a(1 - e^2)}{1 + e\cos(v)}$$

A coordinate transformation is then accomplished to place the position vector in the geocentric frame<sup>3,10</sup>.

The above process determines the position vector of the satellite at a given time. Once this is accomplished, the position of the satellite must be propagated through the orbit by some time step dictated by the user. This is accomplished through the use of the following equations<sup>1</sup>:

$$n = n_0 [1 + 1.5J_2 \frac{(1-e^2)}{p^2} (1 - 1.5\sin^2(i))]$$

$$\Omega = -(1.5J_2 \cos(i))n$$

$$w = (1.5J_2 \frac{[2 - 2.5\sin^2(i)]}{p^2})n$$

These changes in the values of the longitude of the ascending node and the argument of periapsis represent secular perturbations resulting from an aspherical earth.<sup>6</sup> Once these elements are propagated forward, the position vector is recalculated. In order to decrease compounding error, the position vector is propagated each iteration from the original values of  $\Omega$  and  $w$ .

It is important to note other perturbing forces including atmospheric drag were not taken into account for this study. Had drag been included, secular changes in the semi-major axis, eccentricity and the inclination would have been taken into account.<sup>6</sup>

## 5.2 Ground Station Position Determination

For the determination of satellite-ground station visibility periods, the position of the ground station must be calculated. This requires the user know the following information: the year, month, day, hour, minute, and second.

the simulation is to begin, the east longitude and geodetic latitude of the site, and the altitude of the site above mean sea level. This information is used in the determination of the Julian Date, the local sidereal time of the site, and the final calculation of the position vector.

This process begins with the determination of the Julian Date given the year, month, date, and time. The Julian Date is referenced to noon, 1 January 4713 B.C. The equation for the Julian Date used in this program only applies to dates between 1 March 1900 and 28 February 2100<sup>3,10</sup>. The equation is<sup>3</sup>:

$$JD = 367 * \text{Year} - \text{int}\left(\frac{\text{Year} + \text{int}(\text{Month}+9)}{12}\right) + \frac{7(\text{Year} + \text{int}(\text{Month}+9))}{4} + \frac{\text{int}(275 * \text{Month}) + \text{Day} + 1721013.5}{9} + \frac{(\text{Second} + \text{Min})}{60} + \frac{\text{Hour}}{60} - \frac{24}{24}$$

The Julian Date is then used to calculate the Greenwich Sidereal Time at 0 hours UT<sup>3</sup>:

$$\theta_{\text{so}} = 100.4606184 + 36000.77004T_u + .00038793T_u^2$$

$$\text{where } T_u = \frac{\text{Julian Date} - 2451545.0}{36525.0}$$

The Greenwich Sidereal Time is then calculated according to the rotation of the earth and the universal time in terms of angles by<sup>2</sup>:

$$\theta_g = \theta_{\text{so}} + w_e(t - t_0)$$

Finally, the Local Sidereal Time for the site is determined by in terms of angles<sup>2</sup>:

$$\theta = \theta_g + \delta_r$$

From this point, the position vector of the site in the geocentric frame is calculated from<sup>2</sup>:

$$X = \left[ \frac{a_e}{\sqrt{1 - e_e^2 \sin^2(L)}} + H \right] \cos(L)$$

$$Z = \left[ \frac{a_e(1 - e_e^2)}{\sqrt{1 - e_e^2 \sin^2(L)}} + H \right] \sin(L)$$

$$\mathbf{r} = X \cos(\theta) \mathbf{i} + X \sin(\theta) \mathbf{j} + Z \mathbf{k}$$

In a manner similar to the satellite position vector propagation, the site position vector is propagated ahead with respect to the rotation of the earth and the time step indicated. It should be noted that both the satellite position vector and the ground site position vector may be calculated using either a spherical earth or an oblate earth in accordance to the users choice. If an oblate earth is chosen, the K component of both position vectors is scaled by a factor of  $1/\sqrt{1 - e_e^2}$ .

### 5.3 Rise\Set Time Determination

Once the position vectors of the two objects of interest have been determined, the visibility function is calculated at each time step. Although any time step may be specified by the program user, it is suggested 25 second steps be used to allow for computer efficiency.<sup>4</sup> Extremely

large time steps may result in missed rise/set times. In order to insure complete evaluation of the entire time of interest, the position vectors and visibility function are calculated for times one step earlier and one step later than specified by the user. Starting at time equal to zero, parabolic blending is applied to the first four visibility function data points. The equation of the curve between points 2 and 3 is calculated. The real roots of the resulting cubic equation are computed using a closed form root solver<sup>6</sup>. The equations to compute the real roots of a quadratic are included in the program in the event the blended curve is a second degree polynomial or a straight line. All complex roots are ignored for this process. As stated previously, the blended curve is defined by<sup>5</sup>:

$$C(t) = (1 - t)P(r) + tq(s)$$

where  $t$  may take any value between 0 and 1. For this reason, only roots between and including 0 and 1 are considered.

When a real root meeting the above requirements is determined, the coefficients  $a_0$ ,  $a_1$ ,  $a_2$ , and  $a_3$  are recalculated using the times corresponding to points 1, 2, 3 and 4. The roots of the original blended equation are then substituted into this second blended equation. The resulting value of the blended equation is a rise or set time. The root is then increased by a small increment and the value of the second equation is recalculated. If the value is positive, then the root in question represents a

rise time. Similarly, a negative value represents a set time.

The next blended curve is calculated between points 3 and 1 and then checked for roots. This process continues until the entire visibility waveform has been evaluated.

The result is a rise/set history for two objects over a given time period.

#### 5.4 Continuous Visibility Check

As previously mentioned, the final computer program offers the user the option of selecting up to four satellites and four ground stations for evaluation of rise/set times. It is the purpose of the continuous visibility check to evaluate the rise/set history in order to determine if constant communication is possible among the given satellites or between the ground and a constellation of satellites.

There are basically two types of communication links for satellite communications. They are forward/reverse links which occur between satellites, and uplink/downlink occurring between a satellite and the ground<sup>11</sup>. For two satellites, forward/reverse continuous communication is not possible if a rise or set occurs or if the satellites were not in constant communication from the beginning of the evaluation. For a three satellite constellation, at least two paths of visibility out of a possible three must be maintained at all times for constant communication to be

possible. Similarly, four satellites require three paths of visibility out of a possible six. Additionally, checks are made to determine if each ground station is in view of at least one satellite at all times for the purpose of uplink/downlink capabilities.

The continuous visibility check is accomplished by constructing a table containing every rise and set time for each possible communications path. For example, in a three satellite constellation, rise/set times are determined between satellites #1 and #2, #1 and #3, and #2 and #3. The table for this constellation would include all the rise and set times from these satellites. These rise/set opportunities represent critical times since they are the only times during the simulation when the status of visibility can change. In order to accomplish the continuous visibility check, the status of each visibility path must be determined at every rise set time. For the program, a (1) was used if two satellites were visible or experiencing a rise at a given time. Similarly, a (0) was used for a state of no visibility or a set. An example of a three satellite table is shown below.

Time (sec)	Sat's #1 & #2	Sat's #1 & #3	Sat's #2 & #3
0	1	0	1
128	1	0	0
356	0	0	1
700	0	1	0
825	0	1	0
967	1	1	0

As mentioned before, for constant communication to be maintained for a three satellite constellation, at least two paths of visibility must be available at all times. That means the sum of the (1)'s and (0)'s at a given time in the table must be greater than or equal to two. In the example above, communication is broken at 128 seconds and is not re-established until 967 seconds.

The same process is used for a four satellite constellation. In such a case, there are six possible communication paths, and the sum at any given rise or set time must be greater than or equal to three. For ground station to satellite communication, the ground station must be able to communicate with at least one satellite at any time. Therefore, the sum at each rise and set time must be greater than or equal to one for constant communication to be maintained.

## CHAPTER 6

### RESULTS

Attached are the results of three different runs of the final computer program attached in Appendix D. Run #1 represents a validation of the rise/set algorithm of the program. The results of this program were compared to the results contained in the research published in reference one. The initial orbital elements of the four satellites used in the program are found preceding the rise/set times. This run was achieved over a time of 86,400 seconds and a 250 second time step with a spherical earth. These results were almost identical to those achieved by the separate program created by Alfano and Negroni<sup>1</sup>. Also included with the first run results are the rise/set values calculated using the basic iteration method mentioned earlier in the research. For this basic method, a 10,000 second time span was evaluated in 5 second intervals. The greatest variance in the compared results was less than 1 second. It should be noted the computer time to generate the visibility curve for the 10,000 second basic method between two satellites was 12 minutes, while only 3 minutes were required using the parabolic blending method over a 86,400 seconds with a 250 second time step. Run #1 also included a results using a ground station and one satellite. This run involved a 125 second time step over 86,400 seconds and an oblate earth. These results are also found in Appendix A and compare almost identically to those achieved by Alfano and Negroni<sup>1</sup>.

The basic iteration method was applied to this data as well and the results can be found in the adjoining column. The greatest variation between the parabolic blending method and the basic iteration method in this case was approximately 3 seconds.

The results of the second run are included in Appendix B. These results use the same satellites and the ground station from run #1 but all calculations involved the use of an oblate earth. As expected, the oblate earth resulted in earlier rise times and later set times<sup>1</sup>. Additionally, the continuous visibility check was employed in this run. Plots of the visibility function of the ground station versus each of the four satellites is included in this Appendix. Additionally, the combined plot of all four satellite-ground station functions are included as well as the six possible visibility combinations of the four satellites. These combination plots can be used to verify the results of the continuous visibility check.

Appendix C contains data resulting from the third run of the program. This run was intended to check the complete capabilities of the program by using four different satellites and four different ground stations. The run was accomplished over a time span of 86,400 seconds at a time step of 125 seconds. Data for the satellites was chosen randomly from an orbital element ephemeris of actual satellites provided by the United States Space Command. The four ground stations chosen are Space Shuttle tracking

sites. They include<sup>5</sup>: (#1) Kaena Point, Hawaii; (#2) Mahe Island, Indian Ocean; (#3) Thule, Greenland; (#4) Vandenburg Air Force Base, California. Again, the plots of the visibility functions are included and may be used to verify the results of the visibility check. The total run time for this case was approximately twenty minutes.

## CHAPTER 7

### CONCLUSIONS

While the basic iterative technique and Lawton's method are viable solutions to the rise and set time problem, the use of parabolic blending and a closed form solution has many advantages. First, parabolic blending is a flexible means to reconstruct the visibility curve. It can be used with sparse or unequally spaced data and is not restricted to near circular orbits. Second, a closed form root solver allows rise/set times to be calculated directly rather than by an iterative technique thereby reducing computer run time. The resulting timely determination of rise/set times makes this method a useful tool for use with multiple satellites and ground stations. Additionally, the inclusion of a continuous visibility check makes this program a useful tool for the investigation of satellite requirements and space mission design.

LIST OF REFERENCES

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**Appendix A: Program Run #1**

Longitude of the Ascending Node : 0.00000000 DEG  
Argument of Periapsis : 0.00000000 DEG

INITIAL ORBITAL ELEMENTS OF SATELLITE #2:

Eccentricity : 0.9363060000  
Inclination : 64.98740000 DEG  
Mean Anomaly : 0.00000000 DEG  
Longitude of the Ascending Node : 0.00000000 DEG  
Argument of Periapsis : 0.00000000 DEG

INITIAL ORBITAL ELEMENTS OF SATELLITE #3:

Eccentricity : 0.0078742000  
Inclination : 82.87090000 DEG  
Mean Anomaly : 0.00000000 DEG  
Longitude of the Ascending Node : 0.00000000 DEG  
Argument of Periapsis : 0.00000000 DEG

INITIAL ORBITAL ELEMENTS OF SATELLITE #4:

Eccentricity : 0.0048964000  
Inclination : 144.64140000 DEG  
Mean Anomaly : 0.00000000 DEG  
Longitude of the Ascending Node : 0.00000000 DEG  
Argument of Periapsis : 0.00000000 DEG

Rise/Set Times between Satellite #1 and Satellite #2:

83679.13091 SEC - SET

Rise/Set Times between Satellite #1 and Satellite #3:

1450.33207 SEC - SET	1450.222816 SEC
3965.41739 SEC - RISE	3965.454545 SEC
6889.49771 SEC - SET	6889.599589 SEC
9371.13568 SEC - RISE	9371.062356 SEC
12399.31335 SEC - SET	
14774.02357 SEC - RISE	
18419.90807 SEC - SET	
20218.05526 SEC - RISE	
25546.76967 SEC - SET	
27789.37858 SEC - RISE	
30949.66914 SEC - SET	
33360.02044 SEC - RISE	
36352.15032 SEC - SET	
39814.44584 SEC - RISE	
41760.11003 SEC - SET	
44235.69347 SEC - RISE	
47181.56457 SEC - SET	
49643.34461 SEC - RISE	
52636.48892 SEC - SET	
55045.12369 SEC - RISE	
58209.92219 SEC - SET	
60445.55653 SEC - RISE	
65807.11706 SEC - SET	
67619.78663 SEC - RISE	
71227.16594 SEC - SET	
73604.36321 SEC - RISE	
76628.56161 SEC - SET	
79111.00284 SEC - RISE	
82033.93906 SEC - SET	
84549.30712 SEC - RISE	

7692.53382 SEC - SET  
9900.74198 SEC - RISE  
13547.34515 SEC - SET  
13662.27191 SEC - RISE  
19034.87771 SEC - SET  
21382.31557 SEC - RISE  
25086.48497 SEC - SET  
27134.52567 SEC - RISE  
30810.51947 SEC - SET  
32961.40487 SEC - RISE  
36617.71132 SEC - SET  
38842.89352 SEC - RISE  
42484.01314 SEC - SET  
44737.10033 SEC - RISE  
48377.75627 SEC - SET  
50604.70112 SEC - RISE  
54259.69364 SEC - SET  
56413.52413 SEC - RISE  
60087.93877 SEC - SET  
62158.24402 SEC - RISE  
65841.04035 SEC - SET  
67888.41159 SEC - RISE  
71560.14573 SEC - SET  
73673.39260 SEC - RISE  
77319.73512 SEC - SET  
79526.35809 SEC - RISE  
83147.81813 SEC - SET  
85412.55717 SEC - RISE

7692.620000 SEC

28

Rise/Set Times between Satellite #2 and Satellite #3:

2997.87843 SEC - SET	2997.887324 SEC
5931.10222 SEC - RISE	5931.141593 SEC
8939.96295 SEC - SET	8939.946429 SEC
11435.44659 SEC - RISE	
14472.78852 SEC - SET	
16877.79953 SEC - RISE	
19934.36110 SEC - SET	
22297.74182 SEC - RISE	
25367.33066 SEC - SET	
27706.27682 SEC - RISE	
30785.29945 SEC - SET	
33108.06577 SEC - RISE	
36194.14202 SEC - SET	
38505.34408 SEC - RISE	
41597.01520 SEC - SET	
43899.47815 SEC - RISE	
46995.62990 SEC - SET	
49291.29522 SEC - RISE	
52391.13775 SEC - SET	
54681.30707 SEC - RISE	
57784.28440 SEC - SET	
60069.96329 SEC - RISE	
63175.51700 SEC - SET	
65457.45070 SEC - RISE	
68565.29108 SEC - SET	
70844.04327 SEC - RISE	
73953.83055 SEC - SET	
76229.83982 SEC - RISE	
79341.37564 SEC - SET	
81615.05419 SEC - RISE	
84728.03935 SEC - SET	

13412.02208	SEC	- RISE
17536.54531	SEC	- SET
19673.27556	SEC	- RISE
23787.20492	SEC	- SET
25923.63498	SEC	- RISE
30032.62420	SEC	- SET
32169.13711	SEC	- RISE
36275.30607	SEC	- SET
38411.96192	SEC	- RISE
42516.36090	SEC	- SET
44653.14374	SEC	- RISE
48756.32667	SEC	- SET
50893.22948	SEC	- RISE
54995.50864	SEC	- SET
57132.55012	SEC	- RISE
61234.12410	SEC	- SET
63371.29703	SEC	- RISE
67472.30883	SEC	- SET
69609.58623	SEC	- RISE
73710.14286	SEC	- SET
75847.56839	SEC	- RISE
79947.69212	SEC	- SET
82085.26989	SEC	- RISE
86185.16424	SEC	- SET

Rise/Set Times between Satellite #3 and Satellite #4:

728.00260	SEC	- SET	728.253012 SEC
2144.97084	SEC	- RISE	2145.755968 SEC
3508.89011	SEC	- SET	3508.638444 SEC
34217.02408	SEC	- RISE	
35246.56198	SEC	- SET	
36889.15759	SEC	- RISE	
38274.52867	SEC	- SET	
39624.21934	SEC	- RISE	
41174.78140	SEC	- SET	
42839.99372	SEC	- RISE	
43670.74866	SEC	- SET	
72091.70409	SEC	- RISE	
72474.06899	SEC	- SET	
74570.33847	SEC	- RISE	
75735.76905	SEC	- SET	
77179.52589	SEC	- RISE	
78783.75035	SEC	- SET	
80215.31302	SEC	- RISE	
81418.26446	SEC	- SET	
83415.21845	SEC	- RISE	
83937.59649	SEC	- SET	

THE LOCATION OF GROUND STATION =1  
EAST LONGITUDE: 0.000000  
GEODETIC LATITUDE: 39.000000  
ALTITUDE ABOVE THE EARTH ELLIPSOID: 2.900000

## INITIAL ORBITAL ELEMENTS OF SATELLITE =1:

Eccentricity : 0.0078742000  
Inclination : 82.87090000 DEG  
Mean Anomaly : 0.00000000 DEG  
Longitude of the Ascending Node : 0.00000000 DEG  
Argument of Periapsis : 0.00000000 DEG

## RISE AND SET TIMES BETWEEN GROUND STATION #1 AND SATELLITE =1:

366.33816 SEC - RISE	366.4128596 SEC
793.74516 SEC - SET	793.3902878 SEC
5973.86027 SEC - RISE	5972.4175820 SEC
6041.56945 SEC - SET	6044.6470590 SEC
39460.44479 SEC - RISE	
39949.95608 SEC - SET	
44907.37075 SEC - RISE	
45292.93512 SEC - SET	
86361.28564 SEC - RISE	

**Appendix B: Program Run #2**

Rise/Set Times between Satellite #1 and Satellite #3:

1460.52842 SEC - SET  
3954.59411 SEC - RISE  
6901.04371 SEC - SET  
9357.44428 SEC - RISE  
12414.55102 SEC - SET  
14750.81501 SEC - RISE  
18432.45195 SEC - SET  
20059.68746 SEC - RISE  
25578.36179 SEC - SET  
27770.73291 SEC - RISE

Rise/Set Times between Satellite #1 and Satellite #4:

1807.91575 SEC - SET  
4069.57257 SEC - RISE  
7695.00886 SEC - SET  
9900.04560 SEC - RISE  
13549.39377 SEC - SET  
15662.26623 SEC - RISE  
19335.91349 SEC - SET  
21381.74668 SEC - RISE  
25066.47341 SEC - SET  
27132.76382 SEC - RISE

Rise/Set Times between Satellite #2 and Satellite #3:

2997.97685 SEC - SET  
5921.02061 SEC - RISE  
8911.66759 SEC - SET  
11427.18627 SEC - RISE  
11479.19061 SEC - SET  
16808.98772 SEC - RISE  
19941.62420 SEC - SET  
22288.63982 SEC - RISE  
25375.13704 SEC - SET  
27696.99684 SEC - RISE

Rise/Set Times between Satellite #2 and Satellite #4:

4932.42624 SEC - SET  
7104.92257 SEC - RISE  
11273.16055 SEC - SET  
13407.13572 SEC - RISE  
17537.31159 SEC - SET  
19669.08990 SEC - RISE  
23788.08220 SEC - SET  
25919.79045 SEC - RISE

Rise/Set Times between Satellite #3 and Satellite #4:

738.80937 SEC - SET  
2137.92179 SEC - RISE  
3516.84185 SEC - SET

\*

(NOTE: NO ENTRIES OR MESSAGE BELOW INDICATES CONTINUOUS COMMUNICATIONS.)

Communications broken at 3516.84185 SEC  
Communications re-established at 3954.59411 SEC  
Communications broken at 8944.66759 SEC  
Communications re-established at 9357.44428 SEC  
Communications broken at 14479.19061 SEC  
Communications re-established at 14750.81501 SEC  
Communications broken at 19335.91349 SEC  
Communications re-established at 19669.08990 SEC  
Communications broken at 19941.62420 SEC  
Communications re-established at 20069.68746 SEC  
Communications broken at 25375.13704 SEC  
Communications re-established at 27132.76382 SEC

RISE AND SET TIMES BETWEEN GROUND STATION #1 AND

SATELLITE #1:

35

RISE AND SET TIMES BETWEEN GROUND STATION #1 AND

SATELLITE #2:

200.76093 SEC - RISE

3060.09662 SEC - SET

13147.673 SEC - RISE

RISE AND SET TIMES BETWEEN GROUND STATION #1 AND

SATELLITE #3:

366.33816 SEC - RISE

793.74516 SEC - SET

5973.86027 SEC - RISE

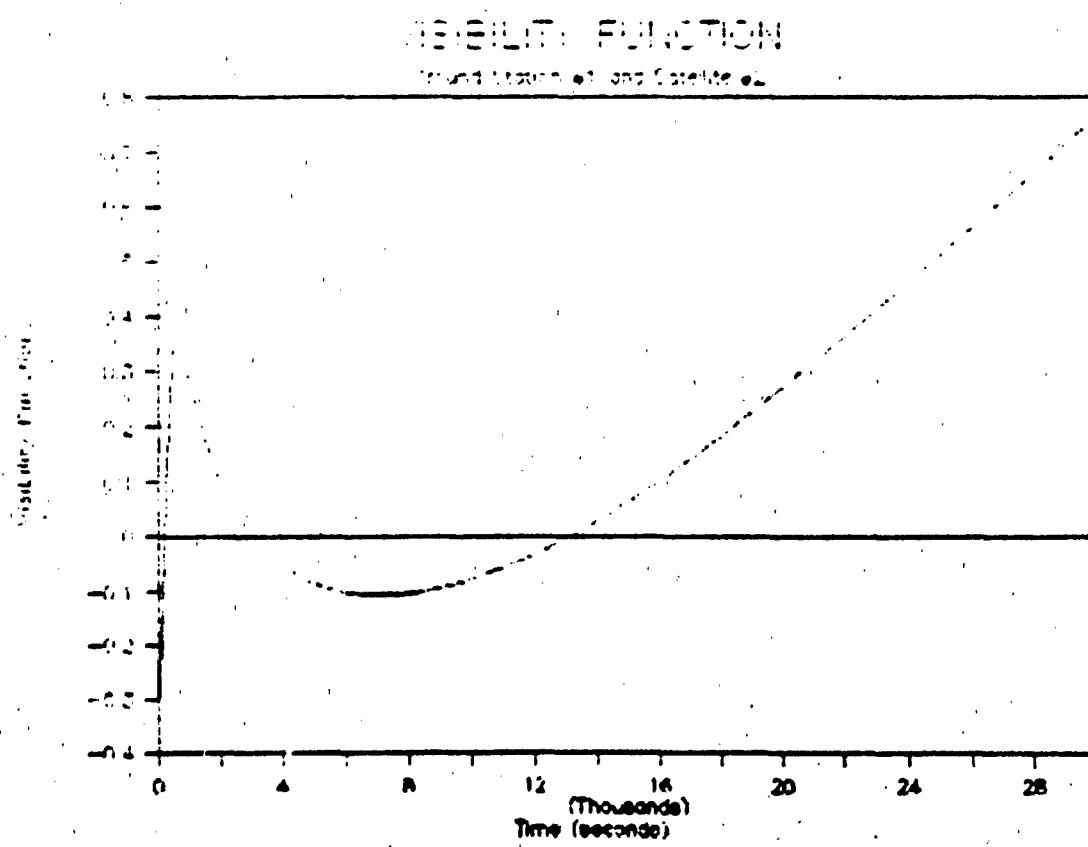
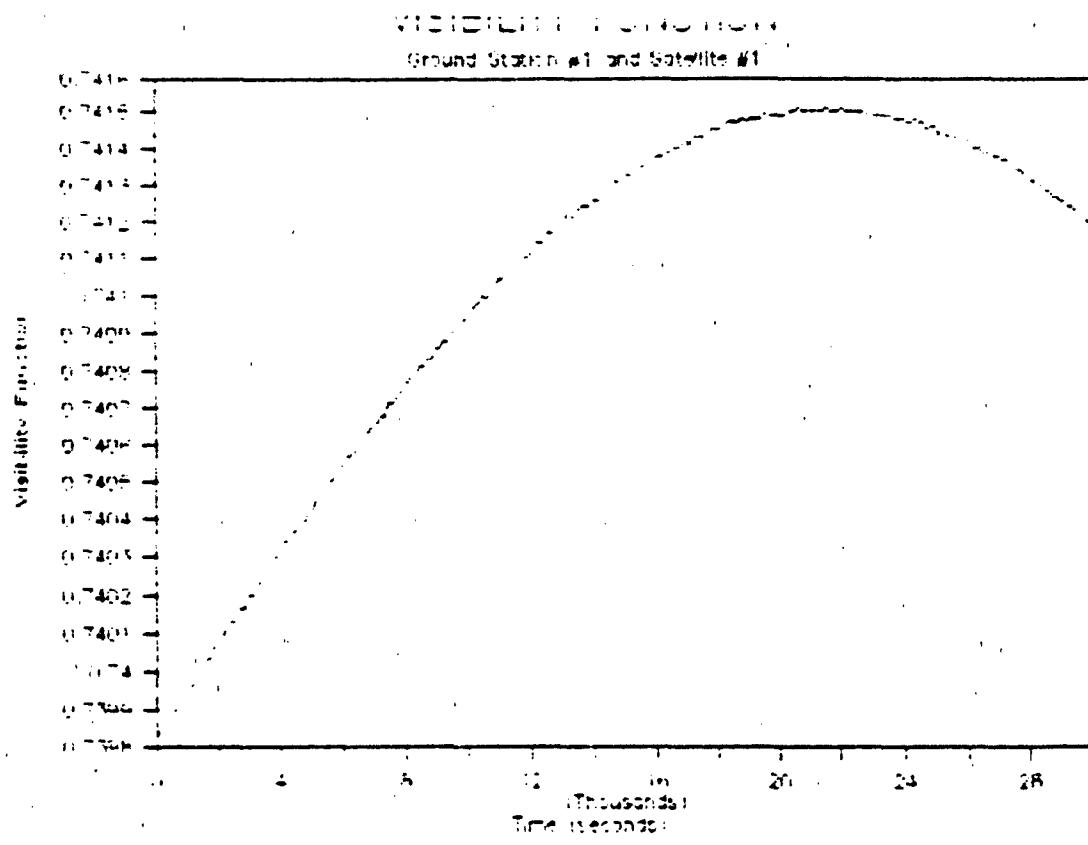
6041.56945 SEC - SET

RISE AND SET TIMES BETWEEN GROUND STATION #1 AND

SATELLITE #4:

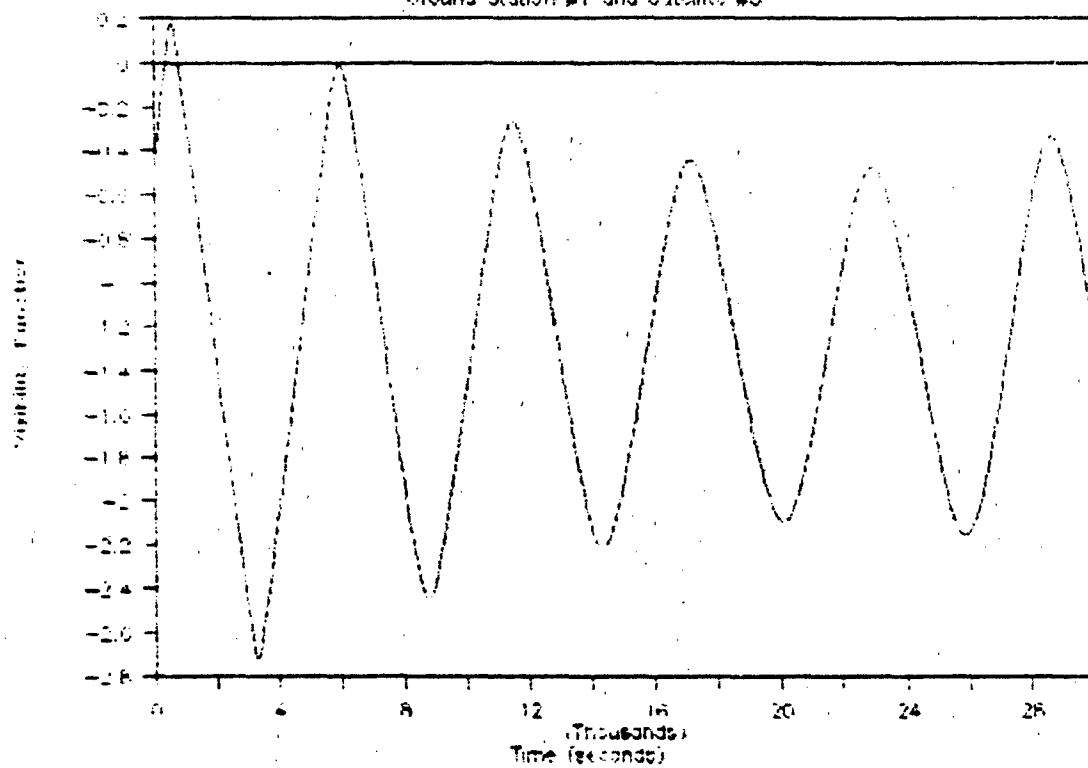
COMMUNICATIONS STATUS BETWEEN GROUND STATION #1 AND THE FOUR GIVEN SATELLITES:

(NOTE: NO ENTRIES OR MESSAGE BELOW INDICATES CONTINUOUS COMMUNICATIONS.)



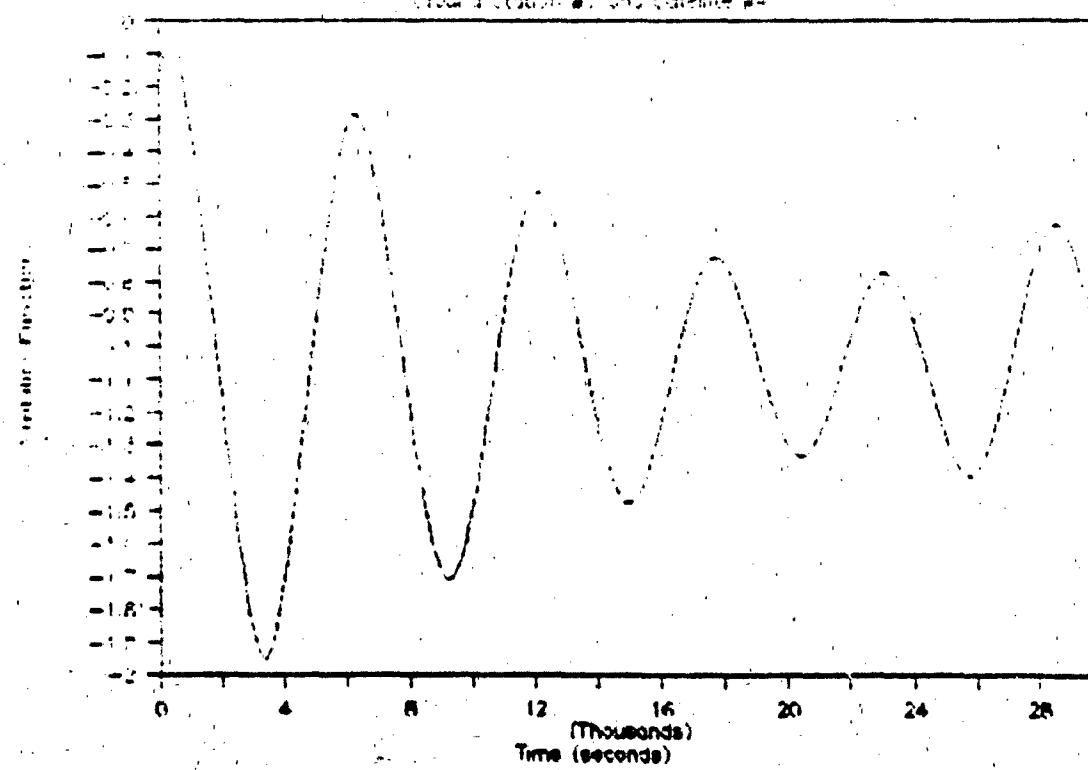
## VISIBILITY FUNCTION

Ground Station #1 and Satellite #3



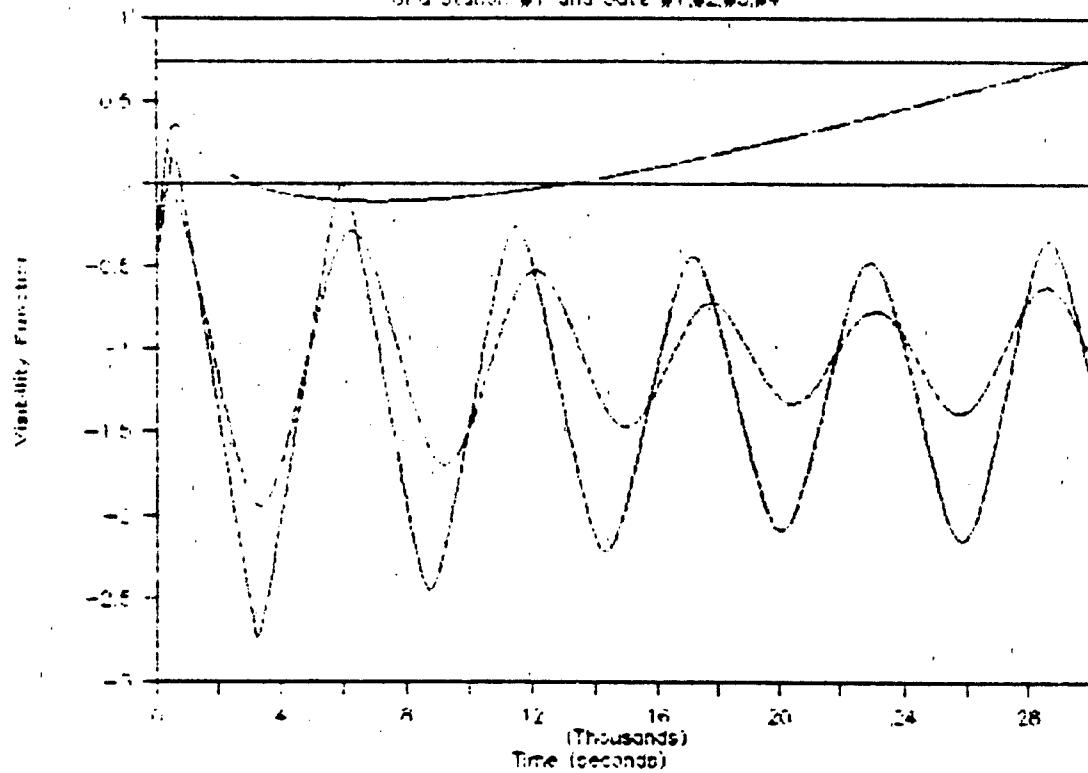
## VISIBILITY FUNCTION

Ground Station #1 and Satellite #4



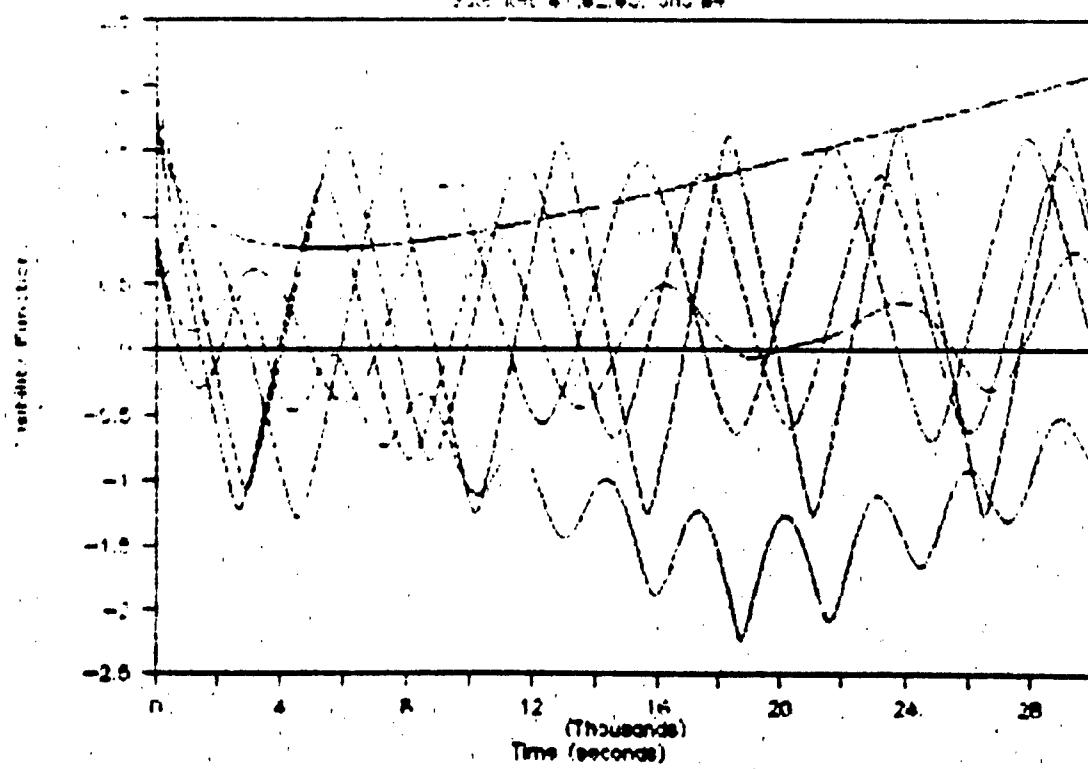
50  
VISIBILITY FUNCTION

Grid Station #1 and Sat's #1, #2, #3, #4



VISIBILITY FUNCTION

Grid Station #1, #2, #3, and #4



**Appendix C: Program Run #3**

TIME FOR BEGINNING THE SIMULATION: 17:30.45

40

THE LOCATION OF GROUND STATION #1

EAST LONGITUDE: 201.735000

GEODETIC LATITUDE: 21.571500

ALTITUDE ABOVE THE EARTH ELLIPSOID: 0.000000

THE LOCATION OF GROUND STATION #2

EAST LONGITUDE: 55.480000

GEODETIC LATITUDE: -4.669900

ALTITUDE ABOVE THE EARTH ELLIPSOID: 0.000000

THE LOCATION OF GROUND STATION #3

EAST LONGITUDE: 291.400000

GEODETIC LATITUDE: 76.508200

ALTITUDE ABOVE THE EARTH ELLIPSOID: 0.000000

THE LOCATION OF GROUND STATION #4

EAST LONGITUDE: 239.498300

GEODETIC LATITUDE: 34.823100

ALTITUDE ABOVE THE EARTH ELLIPSOID: 0.000000

INITIAL ORBITAL ELEMENTS OF SATELLITE #1:

Eccentricity : 0.0668128000

Semi-major Axis : 117819.33914850 KM

Inclination : 57.35000000 DEG

Mean Anomaly : 274.64810000 DEG

Longitude of the Ascending Node : 65.63070000 DEG

Argument of Periapsis : 79.11000000 DEG

INITIAL ORBITAL ELEMENTS OF SATELLITE #2:

Eccentricity : 0.0003109000

Semi-major Axis : 42164.58832806 KM

Inclination : 0.00990000 DEG

Mean Anomaly : 132.80340000 DEG

Longitude of the Ascending Node : 227.28640000 DEG

Argument of Periapsis : 359.92590000 DEG

INITIAL ORBITAL ELEMENTS OF SATELLITE #3:

Eccentricity : 0.0145072000

Semi-major Axis : 7496.14095441 KM

Inclination : 90.26190000 DEG

Mean Anomaly : 246.05610000 DEG

Longitude of the Ascending Node : 107.70380000 DEG

Argument of Periapsis : 115.56590000 DEG

INITIAL ORBITAL ELEMENTS OF SATELLITE #4:

Eccentricity : 0.0531098000

Semi-major Axis : 7210.27162153 KM

Inclination : 66.05630000 DEG

Mean Anomaly : 245.56390000 DEG

Longitude of the Ascending Node : 108.27480000 DEG

Argument of Periapsis : 119.97980000 DEG

\*

Rise/Set Times between Satellite #1 and Satellite #3:

2096.74276 SEC - SET  
3749.77870 SEC - RISE  
8657.22758 SEC - SET  
10396.52711 SEC - RISE  
15206.50054 SEC - SET  
17033.58950 SEC - RISE  
21747.79647 SEC - SET  
23658.24122 SEC - RISE  
28283.42317 SEC - SET

Rise/Set Times between Satellite #1 and Satellite #4:

1307.23847 SEC - SET  
3272.45823 SEC - RISE  
1507.23028 SEC - SET  
9472.56593 SEC - RISE  
13707.25247 SEC - SET  
15679.29431 SEC - RISE  
19906.64430 SEC - SET  
21891.90738 SEC - RISE  
26104.35521 SEC - SET  
28109.37531 SEC - RISE

Rise/Set Times between Satellite #2 and Satellite #3:

9589.46045 SEC - SET  
9952.64793 SEC - RISE  
15090.00549 SEC - SET  
17190.80137 SEC - RISE  
21406.02460 SEC - SET  
23759.34470 SEC - RISE  
27853.51599 SEC - SET

Rise/Set Times between Satellite #2 and Satellite #4:

146.81313 SEC - SET  
2048.36595 SEC - RISE  
7176.32283 SEC - SET  
9093.61752 SEC - RISE  
13570.46290 SEC - SET  
15790.10429 SEC - RISE  
19826.60084 SEC - SET  
22187.89728 SEC - RISE  
26069.57330 SEC - SET  
28469.81596 SEC - RISE

Rise/Set Times between Satellite #3 and Satellite #4:

13706.79928 SEC - SET  
16641.32575 SEC - RISE  
18745.74240 SEC - SET

COMMUNICATIONS STATUS BETWEEN SATELLITE #1, #2, #3, AND #4:  
(NOTE: NO ENTRIES OR MESSAGE BELOW INDICATES CONTINUOUS

COMMUNICATIONS.)

Communications broken at 15090.00549 SEC

Communications re-established at 15790.10429 SEC

Communications broken at 21406.02460 SEC

Communications re-established at 22187.89728 SEC

Communications broken at 27853.51599 SEC

Communications re-established at 28109.37531 SEC

Communications broken at 28283.42317 SEC

Communications re-established at 28469.81596 SEC

\*

27189.14692 SEC - SET

42

RISE AND SET TIMES BETWEEN GROUND STATION #1 AND SATELLITE #2:

RISE AND SET TIMES BETWEEN GROUND STATION #1 AND SATELLITE #3:

6659.66079 SEC - RISE  
7205.64965 SEC - SET  
12742.74680 SEC - RISE  
13876.25363 SEC - SET  
19342.09950 SEC - RISE  
20205.80586 SEC - SET

RISE AND SET TIMES BETWEEN GROUND STATION #1 AND SATELLITE #4:

12011.00325 SEC - RISE  
12888.92281 SEC - SET  
18219.91633 SEC - RISE  
19170.28556 SEC - SET

COMMUNICATIONS STATUS BETWEEN GROUND STATION #1 AND THE FOUR GIVEN SATELLITES:  
(NOTE: NO ENTRIES OR MESSAGE BELOW INDICATES CONTINUOUS COMMUNICATIONS.)

\*

RISE AND SET TIMES BETWEEN GROUND STATION #2 AND SATELLITE #1: 43  
18845.80416 SEC - RISE

RISE AND SET TIMES BETWEEN GROUND STATION #2 AND SATELLITE #2:

RISE AND SET TIMES BETWEEN GROUND STATION #2 AND SATELLITE #3:  
2776.71326 SEC - RISE  
3809.60547 SEC - SET  
9232.43874 SEC - RISE  
10218.11934 SEC - SET

RISE AND SET TIMES BETWEEN GROUND STATION #2 AND SATELLITE #4:  
2575.55488 SEC - RISE  
3233.90819 SEC - SET  
8752.25542 SEC - RISE  
9560.57871 SEC - SET

COMMUNICATIONS STATUS BETWEEN GROUND STATION #2 AND THE FOUR GIVEN SATELLITES:  
(NOTE: NO ENTRIES OR MESSAGE BELOW INDICATES CONTINUOUS COMMUNICATIONS.)

Communications broken at 0.000000000000000  
Communications re-established at 2575.55488485389  
Communications broken at 3809.60546671516  
Communications re-established at 8752.25541685105  
Communications broken at 10218.1193431246  
Communications re-established at 18845.8041619931

\*

RISE AND SET TIMES BETWEEN GROUND STATION #3 AND

SATELLITE #2:

RISE AND SET TIMES BETWEEN GROUND STATION #3 AND

SATELLITE #3:

863.15409 SEC - RISE

1929.46674 SEC - SET

7439.15083 SEC - RISE

8459.80178 SEC - SET

14032.54055 SEC - RISE

15028.79748 SEC - SET

20602.42738 SEC - RISE

21618.43278 SEC - SET

27132.37091 SEC - RISE

28188.78822 SEC - SET

RISE AND SET TIMES BETWEEN GROUND STATION #3 AND

SATELLITE #4:

994.31344 SEC - RISE

1550.61962 SEC - SET

7128.82589 SEC - RISE

7759.49949 SEC - SET

13314.48646 SEC - RISE

13955.25665 SEC - SET

19524.67234 SEC - RISE

20130.86382 SEC - SET

25748.10806 SEC - RISE

26262.61775 SEC - SET

COMMUNICATIONS STATUS BETWEEN GROUND STATION #3 AND THE FOUR GIVEN SATELLITES:

(NOTE: NO ENTRIES OR MESSAGE BELOW INDICATES CONTINUOUS COMMUNICATIONS.)

Communications broken at 0.0000000000000000

Communications re-established at 863.154088411520

Communications broken at 1929.46674256308

Communications re-established at 7128.82589091173

Communications broken at 8459.8017798542

Communications re-established at 13314.4864571971

Communications broken at 13955.2566531969

Communications re-established at 14032.5405513214

Communications broken at 15028.7974810107

Communications re-established at 19524.6723377486

Communications broken at 20130.8638220675

Communications re-established at 20602.4273755799

Communications broken at 21618.4327784578

Communications re-established at 25748.1080570079

Communications broken at 26262.6177511727

Communications re-established at 27132.3709121300

Communications broken at 28188.7882164166

\*

RISE AND SET TIMES BETWEEN GROUND STATION #4 AND SATELLITE #1: 45  
15864.12078 SEC - SET

RISE AND SET TIMES BETWEEN GROUND STATION #4 AND SATELLITE #2:

RISE AND SET TIMES BETWEEN GROUND STATION #4 AND SATELLITE #3:

160.74120 SEC - RISE  
1145.77540 SEC - SET  
6518.52238 SEC - RISE  
7628.58607 SEC - SET  
13356.74253 SEC - RISE  
13863.55253 SEC - SET

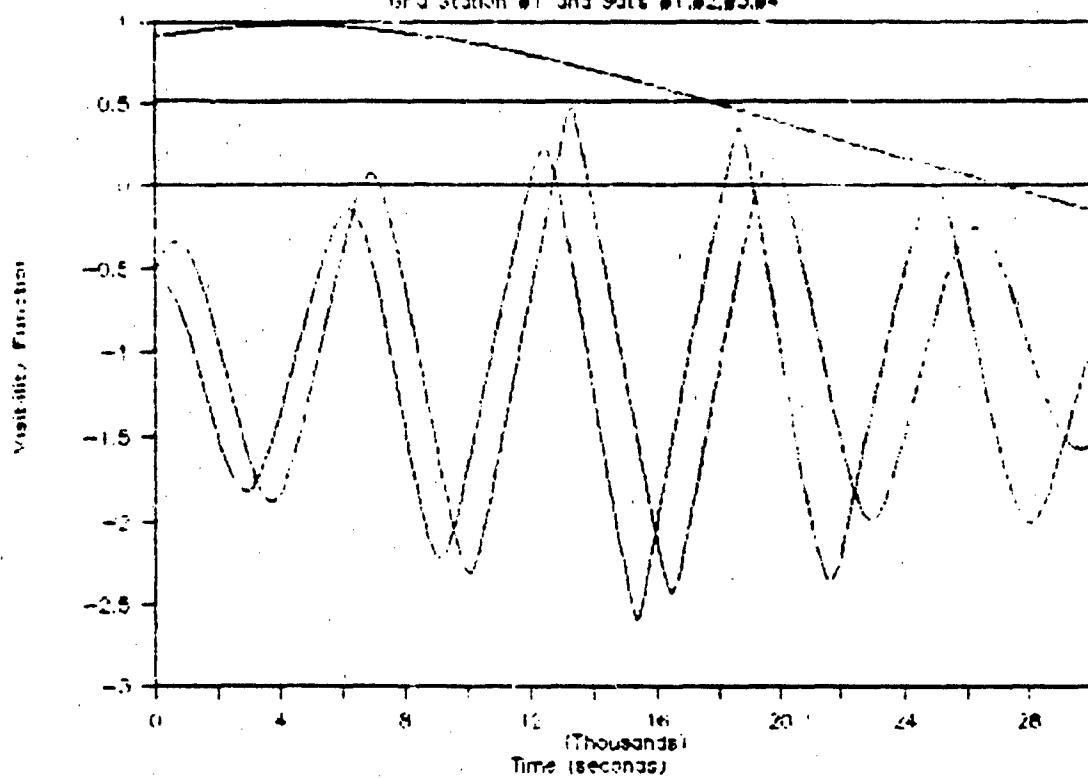
RISE AND SET TIMES BETWEEN GROUND STATION #4 AND SATELLITE #4:

6188.38578 SEC - RISE  
7079.50299 SEC - SET  
12477.73425 SEC - RISE  
13319.74884 SEC - SET  
19231.12443 SEC - RISE  
19321.51031 SEC - SET

COMMUNICATIONS STATUS BETWEEN GROUND STATION #4 AND THE FOUR GIVEN SATELLITES:  
(NOTE: NO ENTRIES OR MESSAGE BELOW INDICATES CONTINUOUS COMMUNICATIONS.)  
Communications broken at 15864.1207815275  
Communications re-established at 19231.1244274451  
Communications broken at 19321.5103139570

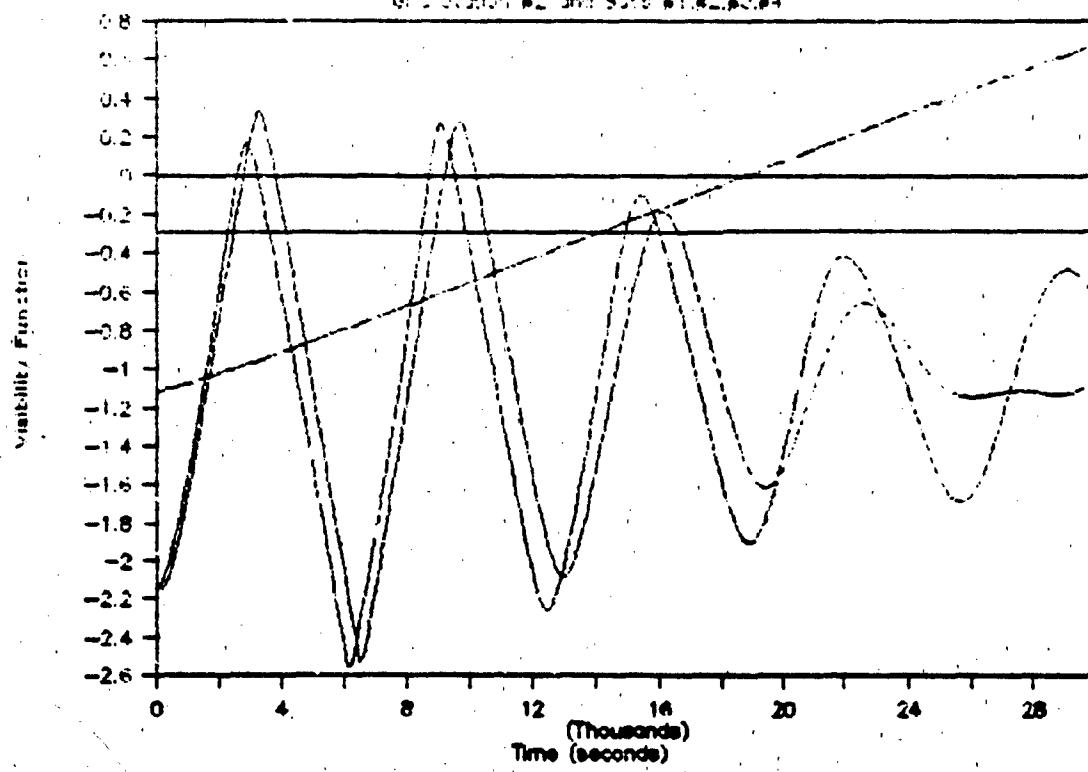
## VISIBILITY FUNCTION: DATA SET #2

Grid Station #1 and Sats #1, #2, #3, #4



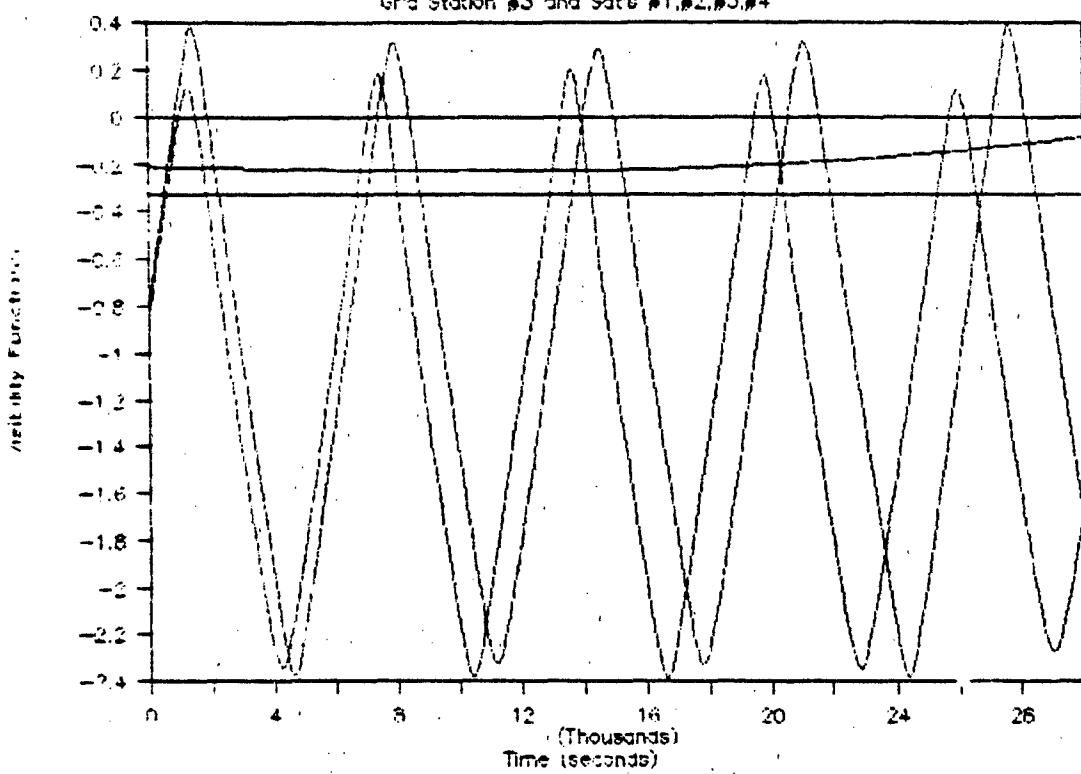
## VISIBILITY FUNCTION: DATA SET #2

Grid Station #2 and Sats #1, #2, #3, #4



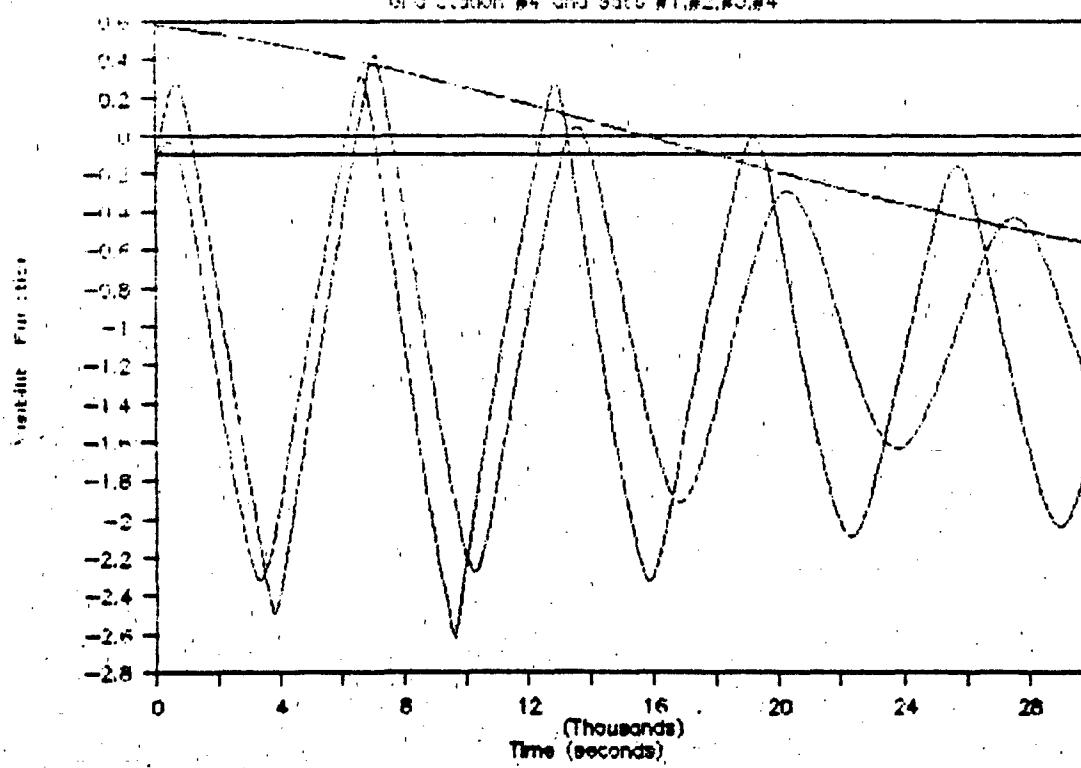
## VISIBILITY FUNCTION: DATA SET #2

Grid Station #3 and Sats #1,#2,#3,#4



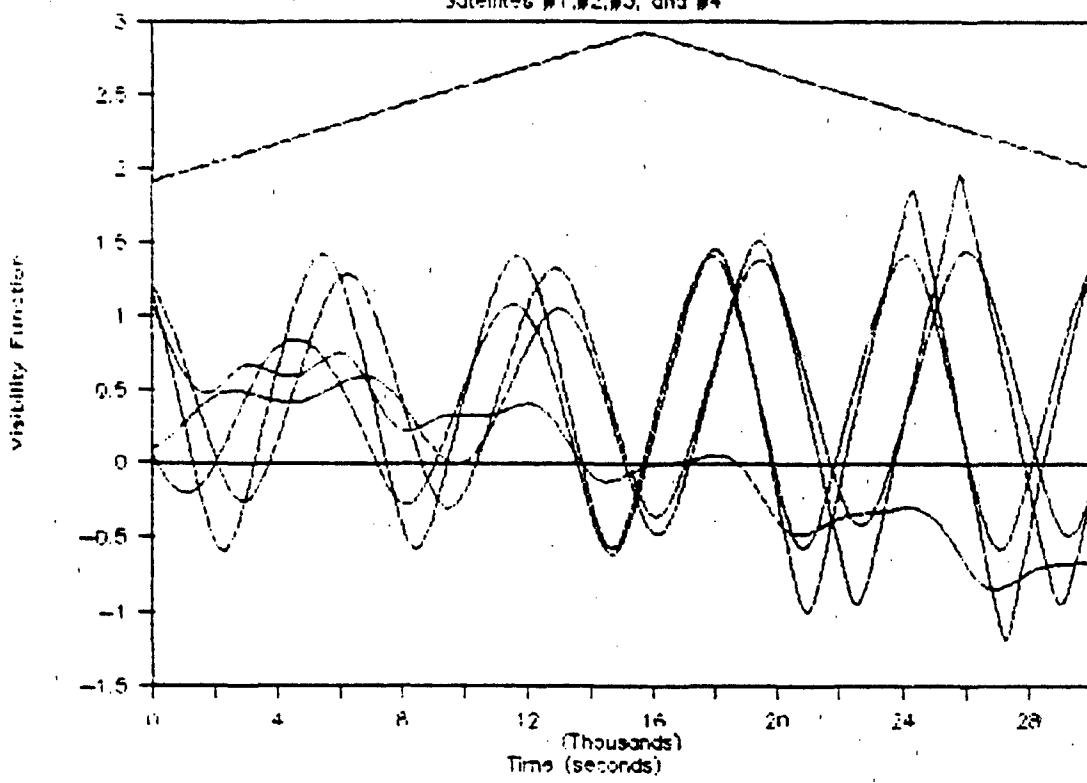
## VISIBILITY FUNCTION: DATA SET #2

Grid Station #4 and Sats #1,#2,#3,#4



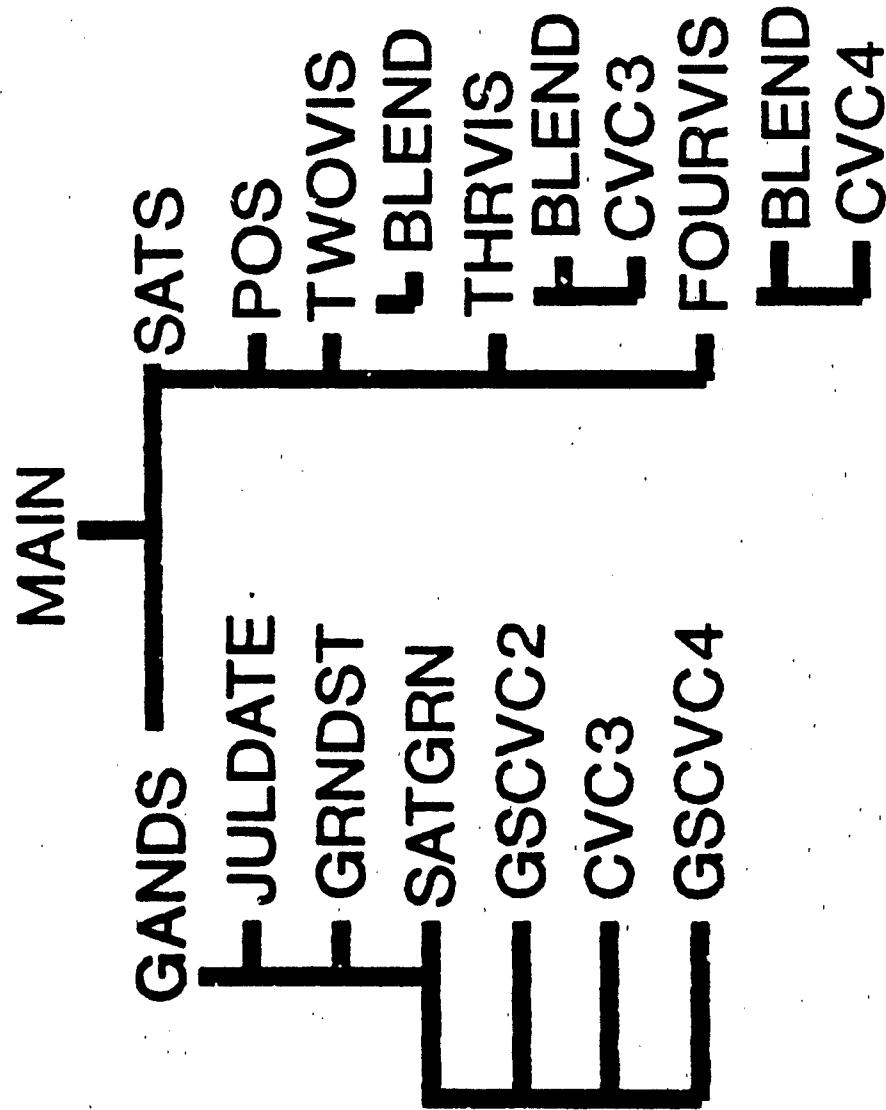
## VISIBILITY FUNCTION: DATA SET #2

Satellites #1, #2, #3, and #4



**Appendix D: Program Listing**

# PROGRAM TREE



\* PURPOSE: This program determines rise set times for inview  
 \* periods for satellite to satellite or satellite to  
 \* ground station viewing. This program is designed  
 \* to accommodate up to four satellites and as many  
 \* ground station. The following information is  
 \* necessary to be able to use the program:  
 \* Satellite Orbit: 1) Eccentricity  
 \*                   2) Length of Semi-major Axis  
 \*                   3) Inclination  
 \*                   4) Mean Anomaly  
 \*                   5) Longitude of the Ascending  
 \*                   Node  
 \*                   6) Argument of Periapsis  
 \* Ground Station: 1) Julian Date in Question  
 \*                   2) East Longitude  
 \*                   3) Height Above Sea Level  
 \* Other required information includes the amount of time  
 \* of interest and the desired time step for incrementa-  
 \* tion. The program is not limited to any particular  
 \* type of orbit. \*changed to mean motion

\* VARIABLES:

\* CHOICE - the number of satellites indicated by the user  
 \* ELIP2 - square of the eccentricity of the earth  
 \* NUM - the number of ground stations indicated by the user  
 \* S2TU - converts SEC to TU; includes the steps size  
 \* SIZE - step size (SEC)  
 \* STEPS - number of steps  
 \* TIME - total time of interest (MIN)  
 \* YORN - yes or no response  
 \* SOROB - spherical or oblate earth

```
*****  
REAL*8 ELIP2,TIME,SIZE,S2TU  
INTEGER CHOICE,NUM,SOROB,STEPS,YORN
```

```
OPEN(UNIT=25,FILE='RISESET.DAT',STATUS='NEW')
```

\*                   USERS CHOICE

```
*****  
WRITE(*,*)' This program is designed to determine rise and'  
WRITE(*,*)'set times for satellite to satellite viewing as well'  
WRITE(*,*)'as satellite to ground station viewing. If you choose'  
WRITE(*,*)'to enter ground stations, satellite to satellite rise'  
WRITE(*,*)'and set times will be computed as well as satellite'  
WRITE(*,*)'to ground station rise and set times.'  
WRITE(*,*)
```

```
1 WRITE(*,*)' Are you interested in satellite to ground station'  
WRITE(*,*)'viewing?      1)Yes      2)No '  
WRITE(*,*)' ***** '  
READ(*,*,ERR=1)YORN
```

```
IF (YORN.GT.2.OR.YORN.LT.1) THEN
```

```
  WRITE(*,*)'Your selection was not a valid response. Please'  
  WRITE(*,*)'select again.'
```

```
  GOTO 5
```

```
ENDIF
```

```
2 WRITE(*,*)'Are you interested in modeling a spherical earth'  
WRITE(*,*)'or an oblate earth? 1)Spherical 2)Oblate'  
WRITE(*,*)' ***** '  
READ(*,*,ERR=2)SOROB
```

```

***** - v.vvv
ELSE IF (SOROB.EQ.2) THEN
    ELIP2 = 0.00669437999013D0
ENDIF
*****
* The following prompts the user to enter the values of the *
* time of interest and the step size. *
*****
5 WRITE(*,*)'What is the total time of interest (in minutes) ==> '
READ(*,*,ERR=5)TIME
WRITE(*,*)'The time entered above will be evaluated in steps.'
WRITE(*,*)'The choice of step size is up to you; however, it '
WRITE(*,*)'should be noted that step sizes too large may result'
WRITE(*,*)'in missed rise and set times. A suggested step size'
WRITE(*,*)'is 250 seconds.'
6 WRITE(*,*)'What is the step size of interest (in secs) ==> '
READ(*,*,ERR=6)SIZE

TIME = TIME*60.0D0
STEPS = DINT(TIME/SIZE)
S2TU = SIZE/806.8103818D0
*****
* The following prompts the user to enter the number of ground *
* stations and/or satellites he/she desires *
*****
IF (YORN.EQ.1) THEN
8   WRITE(*,*)'How many ground stations do you desire. Please'
    WRITE(*,*)'make your selection from below.'
    WRITE(*,*)'    1) 1 Ground Station'
    WRITE(*,*)'    2) 2 Ground Stations'
    WRITE(*,*)'    3) 3 Ground Stations'
    WRITE(*,*)'    4) 4 Ground Stations'
    WRITE(*,*)'====> '
    READ(*,*,ERR=8)NUM

    IF (NUM.LT.1.OR.NUM.GT.4) THEN
        WRITE(*,*)'Your entry was not valid. Please reenter the'
        WRITE(*,*)'number of ground stations.'
        GOTO 8
    ENDIF

9   WRITE(*,*)'How many satellites do you wish to enter? Please'
    WRITE(*,*)'make your selection from below.'
    WRITE(*,*)'    1) 1 Satellite'
    WRITE(*,*)'    2) 2 Satellites'
    WRITE(*,*)'    3) 3 Satellites'
    WRITE(*,*)'    4) 4 Satellites'
    WRITE(*,*)'====> '
    READ(*,*,ERR=9)CHOICE
    CALL GANDS(CHOICE,ELIP2,NUM,S2TU,SIZE,STEPS)

ELSE
10  WRITE(*,*)'Please make a selection for the type of viewing'
    WRITE(*,*)'you prefer:'
    WRITE(*,*)'    1) 2 Satellite Viewing'
    WRITE(*,*)'    2) 3 Satellite Viewing'
    WRITE(*,*)'    3) 4 Satellite Viewing'
    WRITE(*,*)'====> '
    READ(*,*,ERR=10)CHOICE
    NUM = 0

    IF (CHOICE.LT.1.OR.CHOICE.GT.3) THEN
        WRITE(*,*)'Your choice was not valid. Please re-enter'

```

```
CALL SATS(CHOICE,ELIP2,S2TU,SIZE,STEPS)
```

```
ENDIF
```

```
CLOSE(UNIT=10)  
CLOSE(UNIT=11)  
CLOSE(UNIT=12)  
CLOSE(UNIT=13)  
CLOSE(UNIT=14)  
CLOSE(UNIT=15)  
CLOSE(UNIT=25)  
CLOSE(UNIT=31)  
CLOSE(UNIT=32)  
CLOSE(UNIT=33)  
CLOSE(UNIT=34)
```

```
END
```

\* PURPOSE: The purpose of this subroutine is to coordinate the  
\* determination of rise/set times between satellites  
\* and ground stations.  
\*

\* VARIABLES:

\* INPUT:

\* CHOICE - the number of satellites indicated by the user  
\* NUM - the number of ground stations indicated by the user  
\* S2TU - converts SEC to UT  
\* SIZE - step size (SEC)  
\* STEPS - number of steps

\* LOCAL:

\* DAY - 1 to 31  
\* ELIP2 - square of the eccentricity of the earth  
\* ELONG - east longitude position of the ground station  
\* GLAT - geodetic latitude of the ground station  
\* H - altitude above the earth ellipsoid  
\* HOUR - 0 to 23  
\* JD - Julian Date  
\* KIND - determines whether continuous visibility involves  
\* a ground station and three satellites (0) or three  
\* satellites (1)  
\* MIN - 0 to 59  
\* MON - 1 to 12  
\* SEC - 0 to 59  
\* STATE - variable that defines file number  
\* T - time corresponding to a given step  
\* VAR - variable that defines file number  
\* VIS - value of the visibility function at a given step  
\* YEAR - 1900 to 2100

\*\*\*\*\*  
SUBROUTINE GANDS(CHOICE,ELIP2,NUM,S2TU,SIZE,STEPS)

REAL\*8 DAY,ELIP2,ELONG,GLAT,H,HOUR,JD,MIN,MON,S2TU  
REAL\*8 SEC,SIZE,T(0:2005).VIS(0:2005).YEAR  
INTEGER CHOICE,COUNT,IN,INTURN,KIND,NUM,OUT,STATE,STEPS,VAR

OPEN(UNIT=31,FILE='GSPOS1.DAT',STATUS='NEW')  
OPEN(UNIT=32,FILE='GSPOS2.DAT',STATUS='NEW')  
OPEN(UNIT=33,FILE='GSPOS3.DAT',STATUS='NEW')  
OPEN(UNIT=34,FILE='GSPOS4.DAT',STATUS='NEW')

\*\*\*\*\*  
\* In order to accurately determine the position vectors of the \*  
\* given ground station, it is necessary to know the exact time \*  
\* (Universal Time) the simulation is to start. The following \*  
\* lines prompt the user to enter the year, month, day, hour, min- \*  
\* ute, and second the simulation is to start. The Julian Date \*  
\* will be calculated from this information. \*

\*\*\*\*\*  
WRITE(\*,\*)"In order to determine position vectors of the earth"  
WRITE(\*,\*)"ground station(s), it is necessary to know the year,"  
WRITE(\*,\*)"month, day, and time when you wish the simulation to "  
WRITE(\*,\*)"begin. The time of interest is Universal Time."  
WRITE(\*,\*)"Please enter the following information:"

\*\*\*\*\*  
YEAR  
\*\*\*\*\*  
5 WRITE(\*,\*)" What is the year of interest, between 1900 and 2100?"  
WRITE(\*,190)  
READ(\*,\*,ERR=5)YEAR

```
GOTO 5
ENDIF
*****
*          MONTH          *
*****
10 WRITE(*,*)' What is the month of interest? Please enter the '
   WRITE(*,*)' number of the month between 1 and 12.'
   WRITE(*,190)
   READ(*,*,ERR=10)MON
   IF (MON.LT.1.OR.MON.GT.12) THEN
      WRITE(*,*)' The month you entered was not a valid response.'
      WRITE(*,*)' Please re-enter the value.'
      GOTO 10
   ENDIF
*****
*          DAY           *
*****
15 WRITE(*,*)' What is the day of interest? Please enter a value'
   WRITE(*,*)' between 1 and 31.'
   WRITE(*,190)
   READ(*,*,ERR=15)DAY
   IF (DAY.LT.1.OR.DAY.GT.31) THEN
      WRITE(*,*)' The day you entered was not valid. Please'
      WRITE(*,*)' re-enter the value'
      GOTO 15
   ELSE IF (MON.EQ.2.AND.DAY.GT.29) THEN
      WRITE(*,*)'February does not have more than 29 days. Please'
      WRITE(*,*)'reenter the month.'
      GOTO 15
   ELSE IF (DAY.EQ.31) THEN
      IF (MON.EQ.4.OR.MON.EQ.6.OR.MON.EQ.9.OR.MON.EQ.11) THEN
         WRITE(*,*)' The month you entered does not have more than 30'
         WRITE(*,*)' days. Please re-enter the month.'
         GOTO 15
      ENDIF
   ENDIF
*****
*          HOUR          *
*****
20 WRITE(*,*)' What is the hour you wish the simulation to begin?'
   WRITE(*,*)' The value must be between 1 and 23.'
   WRITE(*,190)
   READ(*,*,ERR=20)HOUR
   IF (HOUR.LT.0.OR.HOUR.GT.23) THEN
      WRITE(*,*)' The hour you entered was not valid. Please'
      WRITE(*,*)' re-enter the hour.'
      GOTO 20
   ENDIF
*****
*          MINUTE         *
*****
25 WRITE(*,*)' At what minute in the hour do you wish to begin?'
   WRITE(*,*)' Please enter a number between 1 and 59.'
   WRITE(*,190)
   READ(*,*,ERR=25)MIN
   IF (MIN.LT.0.OR.MIN.GT.59) THEN
      WRITE(*,*)' The minute you entered was not a valid response.'
      WRITE(*,*)' Please re-enter the value.'
      GOTO 25
```

```

*****
30 WRITE(*,*)' At what second do you wish to begin. Please enter'
   WRITE(*,*)' a number between 1 and 59.'
   WRITE(*,190)
   READ(*,*,ERR=30)SEC
   IF (SEC LT.0.OR.SEC.GT.59) THEN
      WRITE(*,*)' The second you entered was not a valid response.'
      WRITE(*,*)' Please re-enter the value.'
      GOTO 30
   ENDIF

   WRITE(25,150)MON,DAY,YEAR
   WRITE(25,160)HOUR,MIN,SEC
   WRITE(25,*)
*****
* The following line calls the subroutine JULDATE where the Julian *
* Date is calculated. *
*****
CALL JULDATE(DAY,HOUR,MIN,MON,SEC,YEAR,JD)
*****
* The following DO loop call for the user to enter the east      *
* longitude and the geodetic latitude. The ground station position *
* vectors are then determined in subroutine GRNDST. *
*****
DO 40 COUNT = 1,NUM
33   WRITE(*,*)'Please enter the east longitude value for the '
   WRITE(*,200)COUNT
   WRITE(*,190)
   READ(*,*,ERR=33)ELONG
   IF (ELONG.LT.-360.0D0.OR.ELONG.GT.360.0D0) THEN
      WRITE(*,*)'The value of longitude entered was not valid.'
      WRITE(*,*)'Please re-enter the value.'
      GOTO 33
   ENDIF
   WRITE(25,220)COUNT
   WRITE(25,230)ELONG
35   WRITE(*,*)'Please enter the geodetic latitude for the '
   WRITE(*,200)COUNT
   WRITE(*,*)'The value should be between -90 and 90 degrees.'
   WRITE(*,190)
   READ(*,*,ERR=35)GLAT

   IF (GLAT.LT.(-90.0D0).OR.GLAT.GT.(90.0D0)) THEN
      WRITE(*,*)'The geodetic latitude value you entered was not'
      WRITE(*,*)'acceptable. Please re-enter the value.'
      GOTO 35
   ENDIF
   WRITE(25,240)GLAT

38   WRITE(*,*)'Please enter the altitude of the ground station '
   WRITE(*,*)'above sea level (in KM).'
   WRITE(*,190)
   READ(*,*,ERR=38)H
   WRITE(25,250)H
   WRITE(25,*)
*****
* Next, the subroutine GRNDST is call where the position vectors of *
* ground station are determined. *
*****
CALL GRNDST(COUNT,ELIP2,ELONG,GLAT,H,JD,S2TU,STEPS)
40 CONTINUE
CLOSE(UNIT=31)
CLOSE(UNIT=32)

```

```

* The subroutine SATS is called in order to determine the rise set *
* times between the satellites entered in this portion of the      *
* program.                                                       *
*****CHOICE = CHOICE - 1
CALL SATS(CHOICE,ELIP2,S2TU,SIZE,STEPS)
CHOICE = CHOICE + 1
*****
* The following opens the necessary files, then records the vis-   *
* ibility data to send to the subroutine BLEND.                  *
*****
DO 70 OUT = 1,NUM
    OPEN(UNIT=60,FILE='TRACKER.DAT',STATUS='UNKNOWN')
    OPEN(UNIT=41,FILE='STAT1.DAT',STATUS='NEW')
    OPEN(UNIT=42,FILE='STAT2.DAT',STATUS='NEW')
    OPEN(UNIT=43,FILE='STAT3.DAT',STATUS='NEW')
    OPEN(UNIT=44,FILE='STAT4.DAT',STATUS='NEW')

VAR = 1

DO 60 IN = 1,CHOICE
    IF (OUT.EQ.1.AND.IN.EQ.1) THEN
        OPEN(UNIT=31,FILE='GSPOS1.DAT',STATUS='OLD')
        OPEN(UNIT=1,FILE='POS1.DAT',STATUS='OLD')
    ELSE IF (OUT.EQ.1.AND.IN.EQ.2) THEN
        OPEN(UNIT=31,FILE='GSPOS1.DAT',STATUS='OLD')
        OPEN(UNIT=2,FILE='POS2.DAT',STATUS='OLD')
    ELSE IF (OUT.EQ.1.AND.IN.EQ.3) THEN
        OPEN(UNIT=31,FILE='GSPOS1.DAT',STATUS='OLD')
        OPEN(UNIT=3,FILE='POS3.DAT',STATUS='OLD')
    ELSE IF (OUT.EQ.1.AND.IN.EQ.4) THEN
        OPEN(UNIT=31,FILE='GSPOS1.DAT',STATUS='OLD')
        OPEN(UNIT=4,FILE='POS4.DAT',STATUS='OLD')

    ELSE IF (OUT.EQ.2.AND.IN.EQ.1) THEN
        OPEN(UNIT=32,FILE='GSPOS2.DAT',STATUS='OLD')
        OPEN(UNIT=1,FILE='POS1.DAT',STATUS='OLD')
    ELSE IF (OUT.EQ.2.AND.IN.EQ.2) THEN
        OPEN(UNIT=32,FILE='GSPOS2.DAT',STATUS='OLD')
        OPEN(UNIT=2,FILE='POS2.DAT',STATUS='OLD')
    ELSE IF (OUT.EQ.2.AND.IN.EQ.3) THEN
        OPEN(UNIT=32,FILE='GSPOS2.DAT',STATUS='OLD')
        OPEN(UNIT=3,FILE='POS3.DAT',STATUS='OLD')
    ELSE IF (OUT.EQ.2.AND.IN.EQ.4) THEN
        OPEN(UNIT=32,FILE='GSPOS2.DAT',STATUS='OLD')
        OPEN(UNIT=4,FILE='POS4.DAT',STATUS='OLD')

    ELSE IF (OUT.EQ.3.AND.IN.EQ.1) THEN
        OPEN(UNIT=33,FILE='GSPOS3.DAT',STATUS='OLD')
        OPEN(UNIT=1,FILE='POS1.DAT',STATUS='OLD')
    ELSE IF (OUT.EQ.3.AND.IN.EQ.2) THEN
        OPEN(UNIT=33,FILE='GSPOS3.DAT',STATUS='OLD')
        OPEN(UNIT=2,FILE='POS2.DAT',STATUS='OLD')
    ELSE IF (OUT.EQ.3.AND.IN.EQ.3) THEN
        OPEN(UNIT=33,FILE='GSPOS3.DAT',STATUS='OLD')
        OPEN(UNIT=3,FILE='POS3.DAT',STATUS='OLD')
    ELSE IF (OUT.EQ.3.AND.IN.EQ.4) THEN
        OPEN(UNIT=33,FILE='GSPOS3.DAT',STATUS='OLD')
        OPEN(UNIT=4,FILE='POS4.DAT',STATUS='OLD')

    ELSE IF (OUT.EQ.4.AND.IN.EQ.1) THEN
        OPEN(UNIT=34,FILE='GSPOS4.DAT',STATUS='OLD')
        OPEN(UNIT=1,FILE='POS1.DAT',STATUS='OLD')

```

```
..... ,STATUS='OLD' /  
ELSE IF (OUT.EQ.4.AND.IN.EQ.3) THEN  
OPEN(UNIT=34,FILE='GSPOS4.DAT',STATUS='OLD')  
OPEN(UNIT=3,FILE='POS3.DAT',STATUS='OLD')  
ELSE IF (OUT.EQ.4.AND.IN.EQ.4) THEN  
OPEN(UNIT=34,FILE='GSPOS4.DAT',STATUS='OLD')  
OPEN(UNIT=4,FILE='POS4.DAT',STATUS='OLD')  
ENDIF  
  
CALL SATGRN(IN,OUT,SIZE,STEPS)  
CLOSE(UNIT=OUT+30)  
CLOSE(UNIT=IN)  
  
OPEN(UNIT=40,FILE='GSVIS.DAT',STATUS='OLD')  
DO 50 INTURN = 1,STEPS+1  
READ(40,*)T(INTURN),VIS(INTURN)  
IF (IN.EQ.1) THEN  
OPEN(UNIT=10,FILE='VIS1.DAT',STATUS='UNKNOWN')  
WRITE(10,*)T(INTURN),VIS(INTURN)  
CLOSE(UNIT=10)  
ELSE IF (IN.EQ.2) THEN  
OPEN(UNIT=11,FILE='VIS2.DAT',STATUS='UNKNOWN')  
WRITE(11,*)T(INTURN),VIS(INTURN)  
CLOSE(UNIT=11)  
ELSE IF (IN.EQ.3) THEN  
OPEN(UNIT=12,FILE='VIS3.DAT',STATUS='UNKNOWN')  
WRITE(12,*)T(INTURN),VIS(INTURN)  
CLOSE(UNIT=12)  
ELSE IF (IN.EQ.4) THEN  
OPEN(UNIT=13,FILE='VIS4.DAT',STATUS='UNKNOWN')  
WRITE(13,*)T(INTURN),VIS(INTURN)  
CLOSE(UNIT=13)  
ENDIF  
50 CONTINUE  
  
WRITE(25,*)  
WRITE(25,260)OUT,IN  
CLOSE(UNIT = 40)  
  
STATE = VAR+40  
CALL BLEND(STATE,STEPS,T,VIS)  
CLOSE(UNIT=STATE)  
VAR=VAR+1  
  
60 CONTINUE  
IF (CHOICE.EQ.2) THEN  
WRITE(25,*)  
WRITE(25,265)OUT  
WRITE(25,285)  
STATE = 41  
CALL GSSCVC2(STATE)  
ELSE IF (CHOICE.EQ.3) THEN  
WRITE(25,*)  
WRITE(25,270)OUT  
WRITE(25,285)  
KIND = 0  
STATE = 41  
CALL CVC3(KIND,STATE)  
ELSE IF (CHOICE.EQ.4) THEN  
WRITE(25,*)  
WRITE(25,280)OUT  
WRITE(25,285)  
STATE = 41  
CALL GSSCVC4(STATE)
```

70 CONTINUE

RETURN

```
150 FORMAT('DATE FOR BEGINNING THE SIMULATION: ',I2,'/',I2,'/',I4)
160 FORMAT('TIME FOR BEGINNING THE SIMULATION: ',I2,':',I2,':',I2)
190 FORMAT(2X,'====> ')
200 FORMAT(' location of ground station #',I1,'.')
220 FORMAT('THE LOCATION OF GROUND STATION #',I1)
230 FORMAT('EAST LONGITUDE: ',F12.6)
240 FORMAT('GEODETIC LATITUDE: ',F12.6)
250 FORMAT('ALTITUDE ABOVE THE EARTH ELLIPSOID: ',F12.6)
260 FORMAT('RISE AND SET TIMES BETWEEN GROUND STATION #',I1,' AND
+ SATELLITE #',I1,':')
265 FORMAT('COMMUNICATIONS STATUS BETWEEN GROUND STATION #',I1,' AND
+ THE TWO GIVEN SATELLITES: ')
270 FORMAT('COMMUNICATIONS STATUS BETWEEN GROUND STATION #',I1,' AND
+ THE THREE GIVEN SATELLITES: ')
280 FORMAT('COMMUNICATIONS STATUS BETWEEN GROUND STATION #',I1,' AND
+ THE FOUR GIVEN SATELLITES: ')
285 FORMAT('(NOTE: NO ENTRIES OR MESSAGE BELOW INDICATES CONTINUOUS
+ COMMUNICATIONS.)')
END
```

\*

\*  
\* PURPOSE: The purpose of this subroutine is to determine the  
\* visibility function between a given satellite and a  
\* given ground station.  
\*

\* VARIABLES:  
\*

INPUT:

\* IN - do loop counter representing the number of sat's  
\* OUT - do loop counter representing the number of ground  
\* stations  
\* SIZE - step size  
\* STEPS - total number of steps

\* LOCAL:

\* COUNT - do loop counter  
\* PHI - angle between the position vector to the satellite  
\* and the position vector to the ground station  
\* R1 - position vector to the ground station  
\* R2 - position vector to the satellite  
\* VIS - value of the visibility function between satellite  
\* and ground station

\* REFERENCES: Lawson, 32

Alfano, Negron, and Moore, 2

\*\*\*\*\*  
SUBROUTINE SATGRN(IN,OUT,SIZE,STEPS)

REAL\*8 PHI,R1(4),R2(4),SIZE,VIS  
INTEGER COUNT,IN,OUT,STEPS

\*\*\*\*\*  
\* GSVIS.DAT contains visibility data between the given satellite and \*  
\* ground station. This file will be overwritten each time SATGRN is \*  
\* called.

\*\*\*\*\*  
OPEN(UNIT=40,FILE='GSVIS.DAT',STATUS='UNKNOWN')  
DO 20 COUNT = 0,STEPS

\*\*\*\*\*  
READ(OUT+30,\*)R1(1),R1(2),R1(3),R1(4)  
READ(IN,\*)R2(1),R2(2),R2(3),R2(1)

\*\*\*\*\*  
\* The next lines define the visibility function between the satellite\*  
\* and the ground station.

\* Reference: Lt Col Salvatore Alfano

\*\*\*\*\*  
PHI = ((R1(1)\*R2(1))+(R1(2)\*R2(2))+(R1(3)\*R2(3)))/(R1(4)\*R2(1))

\*\*\*\*\*  
IF (PHI.GT.(1.0D0)) THEN  
PHI = 1.0D0  
ELSE IF (PHI.LT.(-1.0D0)) THEN  
PHI = -1.0D0  
ENDIF

VIS = DACOS((R1(4))/R2(4)) - DACOS(PHI)

WRITE(40,110)COUNT\*SIZE,VIS

20 CONTINUE

CLOSE(UNIT=40)

RETURN

I10 FORMAT(I10,5X,F12.5)

END

\*

\*\*\*\*\*  
\* SUBROUTINE JULDATE  
\* \*\*\*\*\*

\* PURPOSE: The purpose of this subroutine is to convert conventional time to Julian Date.  
\*

\* VARIABLES:  
\*

INPUT:

\* DAY - 1 to 31  
\* HR - 0 to 23  
\* MIN - 0 to 59  
\* MON - 1 to 12  
\* SEC - 0 to 59  
\* YEAR - 1900 to 2100

OUTPUT:

\* JD - Julian Date  
\*

\* Reference: Valado, 1

\*\*\*\*\*  
SUBROUTINE JULDATE(DAY,HOUR,MIN,MON,SEC,YEAR,JD)

REAL\*8 DAY,HOUR,MIN,MON,SEC,YEAR,JD

JD = 367.0D0\*(YEAR)-DINT((7.0D0\*(YEAR+DINT((MON+9.0D0)/12.0D0)))  
+ /4.0D0)+DINT((275.0D0\*MON)/9.0D0)+DAY+1721013.5D0+  
+ (((SEC/60.0D0)+MIN)/60.0D0)+HOUR)/24.0D0

RETURN  
END  
\*

\* \* \* \* \*  
\* \* \* \* \*  
\* SUBROUTINE GRNDST  
\* \* \* \* \*

\* PURPOSE: The purpose of this subroutine is to determine the  
\* geocentric position of a ground station given Julian  
\* Date, east longitude, and geodetic latitude.  
\* \* \* \* \*

\* VARIABLES:  
\* \* \* \* \*

\* INPUT:  
\* \* \* \* \*

\* ELIP2 - square of the eccentricity of the earth  
\* ELONG - east longitude of the station of interest  
\* GLAT - geodetic longitude of the station of interest  
\* H - altitude of the station above the earth ellipsoid  
\* JD - Julian Date  
\* S2TU - converts SEC to TU  
\* STEPS - number of steps  
\* \* \* \* \*

\* LOCAL VARIABLES:  
\* \* \* \* \*

\* COSLAT - cosine of the geodetic latitude  
\* DEGRAD - conversion from degrees to radians  
\* DENOM - denominator of the equation to determine G1 and G2  
\* DT - change in time  
\* GLAT - geodetic latitude of the ground station  
\* GSR(1-4) - position vectors of the ground station  
\* KM2DU - conversion from km to DU  
\* REP - counter for do loop  
\* SINLAT - sine of the geodetic latitude  
\* TGO - Greenwich Sidereal Time at 0 hr Universal Time  
\* THETA - observers local sidereal time  
\* THETDOT - time rate of change of the local sidereal time  
\* based on the rotation of the earth (rad/TU)  
\* THETG - sidereal time of the Greenwich Meridian  
\* TU - time measured in centuries  
\* TWOPI - two times pi  
\* X - variable for the determination of station position  
\* vector  
\* \* \* \* \*

\* Reference: Valado, 2-4  
\* Bates, Mueller, and White, 98-103  
\* Escobal, 20-21  
\* Alfano, Negron, and Moore, 6

\*\*\*\*\*  
\* SUBROUTINE GRNDST(COUNT,ELIP2,ELONG,GLAT,H,JD,S2TU,STEPS)

REAL\*8 COSLAT,DEGRAD,DENOM,DT,ELIP2,ELONG,GLAT  
REAL\*8 GSR(4),H,JD,KM2DU,S2TU,SINLAT,TGO  
REAL\*3 THETA,THETDOT,THETG,TU,TWOPI,X  
INTEGER COUNT,REP,STEPS

\*\*\*\*\*  
\* CONSTANTS  
\*\*\*\*\*

TWOPI = 2.0D0\*DACOS(-1.0D0)  
DEGRAD = TWOPI/360.0D0  
KM2DU = (1.0D0/6378.137D0)

ELONG = ELONG\*DEGRAD  
GLAT = GLAT\*DEGRAD  
H = H\*KM2DU

THETDOT = .058833590688786D0

\*\*\*\*\*  
\* The following lines calculate the Greenwich Sidereal Time and  
\* to be used in the determination of the Local Sidereal Time.  
\*\*\*\*\*

```

TU      = (DINT(JD) + .5D0 - 2451545.0D0)/36525.0D0
TGO     = 1.753368559D0+628.3319705D0*TU+
+       .0C0006770708127D0*(TU**2.0D0)+(6.30038809866571)*
+       DBLE(JD-DINT(JD)-.5D0)

TGO     = DMOD(TGO,TWOPI)
IF (TGO.LT.(0.0D0)) THEN
    TGO = TWOPI+TGO
ENDIF

DENOM  = DSQRT(1.0D0-(ELIP2*(SINLAT**2.0D0)))

X      = ((1.0D0/DENOM)+H)*COSLAT
GSR(3) = (((1.0D0-ELIP2)/DENOM)+H)*SINLAT*(1.0D0/
+       DSQRT(1.0D0-ELIP2))
GSR(4) = DSQRT((X**2.0D0)+(GSR(3)**2.0D0))

TGO = 0.0D0
*****
*   The following lines calculate the x and z variables for the      *
*   position of the ground station. These variables are then used   *
*   to calculate the position vector in the IJK or geocentric coor-   *
*   dinate system.                                                 *
*****
DO 50 REP = 0,STEPS
    DT   = REP*S2TU
    THETG = TGO + THETDOT*DT
    THETA = THETG + ELONG

    GSR(1) = X*DCOS(THETA)
    GSR(2) = X*DSIN(THETA)

    WRITE(COUNT+30,100)GSR(1),GSR(2),GSR(3),GSR(4)

50 CONTINUE
RETURN

100 FORMAT(F12.5,5X,F12.5,5X,F12.5,5X,F12.5)

END

```

## SUBROUTINE SATS

**PURPOSE:**

## VARIABLES:

### ORBITAL ELEMENTS:

ARGP	- argument of periapsis for $\oplus$ orbit	(DEG)
AXIS	- semi-major axis for $\oplus$ orbit	(KM)
ECC	- eccentricity for $\oplus$ orbit	
INC	- inclination for $\oplus$ orbit	(DEG)
MA	- mean anomoly for $\oplus$ orbit	(DEG)
NODE	- longitude of the ascending node for $\oplus$ orbit	(DEG)

#### **OTHER VARIABLES:**

AKM	- value of the semi-major axis in KM
CHOICE	- reflects the users choice for operation
COUNT	- DO loop counter
D2RAD	- converts DEG to RAD
DU2KM	- converts DUs to KM
ELIP2	- square of the eccentricity of the earth
KIND	- differentiates between a ground station and three satellites (0) and three satellites (1)
N	- mean motion of the satellites (DU/T)
S2TU	- converts SEC to TU
SIZE	- step size (SEC)
STATE	- file number
STEPS	- number of steps
T	- chronological time over time span
TWOPi	- twice the value of pi
VIS	- value of the visibility function

SUBROUTINE SATS(CHOICE,ELIP2,S2TU,SIZE,STEPS)

```

REAL*8 AKM,ARGP,AXIS,D2RAD,DU2KM,ECC,ELIP2,INC,MA,NODE
REAL*8 S2TU,SIZE,T(0:500),TWOP1,VIS(0:500),N
INTEGER CHOICE,COUNT,KIND,STATE,STEPS

```

```
OPEN(UNIT=1,FILE='POS1.DAT',STATUS='NEW')
OPEN(UNIT=2,FILE='POS2.DAT',STATUS='NEW')
OPEN(UNIT=3,FILE='POS3.DAT',STATUS='NEW')
OPEN(UNIT=4,FILE='POS4.DAT',STATUS='NEW')
OPEN(UNIT=60,FILE='TRACKER.DAT',STATUS='NEW')
```

## CONSTANTS

**TWOPI** = 2.000\*DACOS(-1.00)  
**D2RAD** = (TWOPI/360.00)  
**D12EM** = 6378.13700

- \* The following prompts the user to enter the values of the orbital elements for the satellites of interest.

DO 20 COUNT = 1,CHOICE+1  
ECC = 0.0D0  
AXIS = 0.0D0  
INC = 0.0D0  
MA = 0.0D0  
NODE = 0.0D0  
ARGP = 0.0D0  
N = 0.0D0

**WRITE(25,510)COUNT**

```

        WRITE(25,520)ECC
12      WRITE(*,*)"Mean Motion (rev/day) ==> "
        READ(*,*,ERR=12)N
          N = N*.05867301522d0
          AXIS = (1.0D0/(N**2.0D0))**(.333333D0)
          AKM = AXIS*DU2KM
          WRITE(25,530)AKM
13      WRITE(*,*)"Inclination ==> "
        READ(*,*,ERR=13)INC
        WRITE(25,540)INC
14      WRITE(*,*)"Mean Anomaly (DEG) ==> "
        READ(*,*,ERR=14)MA
        WRITE(25,550)MA
15      WRITE(*,*)"Longitude of the Ascending Node (DEG) ==> "
        READ(*,*,ERR=15)NODE
        WRITE(25,560)NODE
16      WRITE(*,*)"Argument of Periapsis (DEG) ==> "
        READ(*,*,ERR=16)ARGP
        WRITE(25,570)ARGP
        WRITE(25,*)
        WRITE(*,*)
        WRITE(*,*)"Please stand-by. Calculations are in progress."
        WRITE(*,*)
*****
```

```

* The following converts the values entered from KM to DU, or from *
* DEG to RAD. *
```

```

INC = INC*D2RAD
MA = MA*D2RAD
NODE = NODE*D2RAD
ARGP = ARGP*D2RAD
```

```

CALL POS(COUNT,ELIP2,S2TU,STEPS,AXIS,ECC,INC,N,NODE,ARGP,MA)
CLOSE(UNIT = COUNT)
```

20 CONTINUE

```

IF (CHOICE.EQ.0) THEN
  GOTO 400
ENDIF
```

```

*****
```

```

* In the following if loop, the computer calls the subroutine *  

* necessary to check all options of visibility depending on the *  

* number of satellites in consideration. *
```

```

*****
```

```

*      2 SATELLITES *
```

```

*****
```

```

WRITE(*,*)"The computer is in the process of determining vis"
WRITE(*,*)"and set times. Please stand by."
```

```

IF (CHOICE.EQ.1) THEN
  CALL TWOVIS(STEPS,SIZE)
  OPEN(UNIT=10,FILE='VIS1.DAT',STATUS='OLD')
  DO 30 COUNT = 1,STEPS+1
    READ(10,*)T(COUNT),VIS(COUNT)
```

30 CONTINUE  
 CLOSE(UNIT=10)  
 WRITE(25,\*)  
 WRITE(25,600)

```

STATE = 41
OPEN(UNIT=41,FILE='STAT1.DAT',STATUS='NEW')
CALL BLEND(STATE,STEPS,T,VIS)
```

```

*****
ELSE IF (CHOICE.EQ.2) THEN
  CALL THRVIS(STEPS,SIZE)
  OPEN(UNIT=10,FILE='VIS1.DAT',STATUS='OLD')
  DO 40 COUNT = 1,STEPS+1
    READ(10,*)T(COUNT),VIS(COUNT)
40  CONTINUE
  CLOSE(UNIT=10)
  WRITE(25,*)
  WRITE(25,600)

  STATE = 41
  OPEN(UNIT=41,FILE='STAT1.DAT',STATUS='NEW')
  CALL BLEND(STATE,STEPS,T,VIS)
  CLOSE(UNIT=41)

  OPEN(UNIT=11,FILE='VIS2.DAT',STATUS='OLD')
  DO 50 COUNT = 1,STEPS+1
    READ(11,*)T(COUNT),VIS(COUNT)
50  CONTINUE
  CLOSE(UNIT=11)
  WRITE(25,*)
  WRITE(25,630)

  STATE=42
  OPEN(UNIT=42,FILE='STAT2.DAT',STATUS='NEW')
  CALL BLEND(STATE,STEPS,T,VIS)
  CLOSE(UNIT=42)

  OPEN(UNIT=12,FILE='VIS3.DAT',STATUS='OLD')
  DO 60 COUNT = 1,STEPS+1
    READ(12,*)T(COUNT),VIS(COUNT)
60  CONTINUE
  CLOSE(UNIT=12)
  WRITE(25,*)
  WRITE(25,620)

  STATE=43
  OPEN(UNIT=43,FILE='STAT3.DAT',STATUS='NEW')
  CALL BLEND(STATE,STEPS,T,VIS)
  CLOSE(UNIT=43)
  CLOSE(UNIT=60)

  KIND = 1
  STATE=41
  WRITE(25,*)
  WRITE(25,660)
  WRITE(25,665)
  CALL CVC3(KIND,STATE)
****

*        4 SATELLITES
****

ELSE IF (CHOICE.EQ.3) THEN
  CALL FOURVIS(STEPS,SIZE)
  OPEN(UNIT=10,FILE='VIS1.DAT',STATUS='OLD')
  DO 70 COUNT = 1,STEPS+1
    READ(10,*)T(COUNT),VIS(COUNT)
70  CONTINUE
  CLOSE(UNIT=10)
  WRITE(25,*)
  WRITE(25,600)

  STATE=41

```

```
OPEN(UNIT=11,FILE='VIS2.DAT',STATUS='OLD')
DO 80 COUNT = 1,STEPS+1
  READ(11,*)T(COUNT),VIS(COUNT)
80 CONTINUE
CLOSE(UNIT=11)
WRITE(25,*)
WRITE(25,610)

STATE=42
OPEN(UNIT=42,FILE='STAT2.DAT',STATUS='NEW')
CALL BLEND(STATE,STEPS,T,VIS)
CLOSE(UNIT=42)

OPEN(UNIT=12,FILE='VIS3.DAT',STATUS='OLD')
DO 90 COUNT = 1,STEPS+1
  READ(12,*)T(COUNT),VIS(COUNT)
90 CONTINUE
CLOSE(UNIT=12)
WRITE(25,*)
WRITE(25,620)

STATE=43
OPEN(UNIT=43,FILE='STAT3.DAT',STATUS='NEW')
CALL BLEND(STATE,STEPS,T,VIS)
CLOSE(UNIT=43)

OPEN(UNIT=13,FILE='VIS4.DAT',STATUS='OLD')
DO 100 COUNT = 1,STEPS+1
  READ(13,*)T(COUNT),VIS(COUNT)
100 CONTINUE
CLOSE(UNIT=13)
WRITE(25,*)
WRITE(25,630)

STATE=44
OPEN(UNIT=44,FILE='STAT4.DAT',STATUS='NEW')
CALL BLEND(STATE,STEPS,T,VIS)
CLOSE(UNIT=44)

OPEN(UNIT=14,FILE='VIS5.DAT',STATUS='OLD')
DO 110 COUNT = 1,STEPS+1
  READ(14,*)T(COUNT),VIS(COUNT)
110 CONTINUE
CLOSE(UNIT=14)
WRITE(25,*)
WRITE(25,640)

STATE=45
OPEN(UNIT=45,FILE='STAT5.DAT',STATUS='NEW')
CALL BLEND(STATE,STEPS,T,VIS)
CLOSE(UNIT=45)

OPEN(UNIT=15,FILE='VIS6.DAT',STATUS='OLD')
DO 120 COUNT = 1,STEPS+1
  READ(15,*)T(COUNT),VIS(COUNT)
120 CONTINUE
CLOSE(UNIT=15)
WRITE(25,*)
WRITE(25,650)

STATE=46
OPEN(UNIT=46,FILE='STAT6.DAT',STATUS='NEW')
```

```
STATE=41
WRITE(25,*)
WRITE(25,670)
WRITE(25,665)
CALL CVC4(STATE)

ENDIF

CLOSE(UNIT=60,STATUS='DELETE')

400 CONTINUE

RETURN

500 FORMAT(' elements of satellite #',I1,:')
510 FORMAT('INITIAL ORBITAL ELEMENTS OF SATELLITE #',I1,:')
520 FORMAT(3X,'Eccentricity : ',F12.10)
530 FORMAT(3X,'Semi-major Axis : ',F15.8,' KM')
540 FORMAT(3X,'Inclination : ',F15.8,' DEG')
550 FORMAT(3X,'Mean Anomoly : ',F15.8,' DEG')
560 FORMAT(3X,'Longitude of the Ascending Node : ',F15.8,' DEG')
570 FORMAT(3X,'Argument of Periapsis : ',F15.8,' DEG')
600 FORMAT('Rise/Set Times between Satellite #1 and Satellite #2:')
610 FORMAT('Rise/Set Times between Satellite #1 and Satellite #3:')
620 FORMAT('Rise/Set Times between Satellite #1 and Satellite #4:')
630 FORMAT('Rise/Set Times between Satellite #2 and Satellite #3:')
640 FORMAT('Rise/Set Times between Satellite #2 and Satellite #4:')
650 FORMAT('Rise/Set Times between Satellite #3 and Satellite #4:')
660 FORMAT('COMMUNICATIONS STATUS BETWEEN SATELLITE #1, #2, AND #3:')
665 FORMAT('(NOTE: NO ENTRIES OR MESSAGE BELOW INDICATES CONTINUOUS
+ COMMUNICATIONS.)')
670 FORMAT('COMMUNICATIONS STATUS BETWEEN SATELLITE #1, #2, #3, AND
+ #4:')
END
```

\*

\* SUBROUTINE POS  
 \*  
 \* PURPOSE: The purpose of this subroutine is to determine the  
 \* position of a satellite given the classical orbital  
 \* elements.  
 \*  
 \* VARIABLES:  
 \* INPUT:  
 \* ARGP - argument of periapsis for @ orbit (RAD)  
 \* AXIS - semi-major axis for @ orbit (DU)  
 \* COUNT - DO loop counter; indicates the satellite number  
 \* ECC - eccentricity for @ orbit  
 \* ELIP2 - square of the eccentricity of the earth  
 \* INC - inclination for @ orbit (RAD)  
 \* MA - mean anomoly for @ orbit (RAD)  
 \* NODE - longitude of the ascending node for @ orbit (RAD)  
 \* S2TU - time step (TU)  
 \* STEPS - number of steps in the requested interval  
 \*  
 \* LOCAL VARIABLES:  
 \* COSARGP - cosine of the argument of periapsis  
 \* COSFINALE - final value of the cosine of the eccentric anomoly  
 \* COSINC - cosine of the inclination  
 \* COSNODE - cosine of the longitude of the ascending node  
 \* COSNU - cosine of the true anomoly  
 \* DENOM - variable for the denominator of a given quotient  
 \* DIF - difference between two value of the eccentric  
 \* anomoly during Newton-Rhapson Iteration  
 \* ECOSFE - eccentricity multiplied by the cosine of the  
 \* finale value of the eccentric anomoly  
 \* EN - first value of the eccentric anomoly for use in  
 \* the Newton-Rhapson Iteration  
 \* ENPLUSONE - second value of the eccentric anomoly as  
 \* calculated in the Newton-Rhapson Iteration  
 \* FINALE - final value of the eccentric anomoly reached by  
 \* convergence of the Newton-Rhapson Iteration  
 \* J2 -  
 \* M - value of the mean anomoly at each time step  
 \* MN - value of the mean anomoly calculated using a  
 \* given value for the eccentric anomoly (used in the  
 \* Newton-Rhapson Iteration)  
 \* MULT - matrix used to rotate the position vectors from  
 \* the perifocal reference frame to the geocentric  
 \* reference frame  
 \* N - mean motion of the satellite  
 \* NANOM - anomolistic mean motion  
 \* NEWARGP - propogated argument of periapsis  
 \* NEWNODE - propogated longitude of the ascending node  
 \* P - calculated value of the semi-latus rectum for the  
 \* orbit  
 \* R - calculated position vectors of the satellite  
 \* REP - DO loop counter  
 \* RPQW - position vectors of the satellite in the perifocal  
 \* frame  
 \* SINARGP - sine of the argument of periapsis  
 \* SINFINE - sine of the final value of the eccentric anomoly  
 \* SININC - sine of the inclination of the orbit  
 \* SINNODE - sine of the longitude of the ascending node  
 \* SINNU - sine of the true anomoly  
 \* TWOPI - constant; two multiplied by pi  
 \*  
 \* REFERENCES: Bates, Mueller, and White, 187, 219-222  
 \*\*\*\*=  
 \* SUBROUTINE POS(COUNT,ELIP2,S2TU,STEPS,AXIS,ECC,INC,N,NODE,ARGP,MA)

```

REAL*8 NODEDOT, NODE, NU, P, R(4), RPQW(4), S2TU, SINARGP
REAL*8 SINFINE, SININC, SINNODE, SINNU, TWOPI
INTEGER COUNT, REP, STEPS
*****
* The following computes values of variables which will be used *
* multiple times within the program. This is done to decrease the *
* amount of calculation necessary within the subroutine. *
*****
COSINC = DCOS(INC)
SININC = DSIN(INC)

J2 = .00108262D0
TWOPI = 2.0D0*DACOS(-1.0D0)
P = AXIS*(1.0D0 - (ECC**2.0D0))
N = N*S2TU
*****
* The following calculates the values necessary to propagate the *
* satellite forward in its orbit. *
*****
NANOM = N*(1.0D0+((1.5D0+J2*(DSQRT(1.0D0-(ECC**2.0D0)))/
+ (P**2.0D0))*(1.0D0-(1.5D0*(SININC**2.0D0))))) )
NODEDOT = -(1.5D0*(J2/P**2.0D0)*COSINC)*NANOM
ARGPDT = (1.5D0*(J2/P**2.0D0)*(2.0D0-(2.5D0*
+ (SININC**2.0D0))))*NANOM

DO 50 REP = 0, STEPS
    NEWNODE = DMOD((NODE + (NODEDOT)*REP), TWOPI)
    NEWARGP = DMOD((ARGP + (ARGPDT)*REP), TWOPI)
    COSNODE = DCOS(NEWNODE)
    SINNODE = DSIN(NEWNODE)
    COSARGP = DCOS(NEWARGP)
    SINARGP = DSIN(NEWARGP)
*****
* The following 3x3 matrix is used to transform the position vector*
* from the PQW (perifocal) frame to the IJK (geocentric) frame. *
*****
MULT(1,1) = COSNODE*COSARGP - SINNODE*SINARGP*COSINC
MULT(1,2) = -COSNODE*SINARGP - SINNODE*COSARGP*COSINC
MULT(1,3) = SINNODE*SININC
MULT(2,1) = SINNODE*COSARGP + COSNODE*SINARGP*COSINC
MULT(2,2) = -SINNODE*SINARGP + COSNODE*COSARGP*COSINC
MULT(2,3) = -COSNODE*SININC
MULT(3,1) = SINARGP*SININC
MULT(3,2) = COSARGP*SININC
MULT(3,3) = COSINC
*****
* In the next loop, the Newton-Raphson iteration is carried out in *
* order to determine the value of the eccentric anomaly at every *
* time step in the orbit of the satellite. *
*****
M = DMOD((MA + (NANOM*REP)), TWOPI)
EN = M
10 MN = EN - ECC*(DSIN(EN))
ENPLUSONE = (EN + ((M - MN)/(1.0D0 - (ECC*(DCOS(EN))))))
DIF = DABS(EN - ENPLUSONE)

IF (DIF.GT.(.000001D0)) THEN
    EN = ENPLUSONE
    GOTO 10
ELSE
    FINALE = ENPLUSONE
ENDIF

```

```

ECOSFE = ECC*COSFINE
DENOM  = AXIS*(1.0D0 - (ECC*COSFINE))

COSNU = (ECC - COSFINE)/(ECOSFE - 1.0D0)
SINNU = ((AXIS*(DSQRT(1.0D0 - ECC**2.0D0)))*SINFINE)/DENOM
NU    = DATAN2(SINNU,COSNU)

COSNU = DCOS(NU)
SINNU = DSIN(NU)
*****
* In the next three lines, the position vector in the perifocal      *
* coordinate system is calculated.                                     *
*****
RPQW(1) = (P*COSNU)/(1.0D0 + (ECC*COSNU))
RPQW(2) = (P*SINNU)/(1.0D0 + (ECC*COSNU))
RPQW(3) = 0.0D0
*****
* The next lines transform the RPQW vector to the geocentric      *
* coordinate frame.                                                 *
*****
R(1) = RPQW(1)*MULT(1,1) + RPQW(2)*MULT(1,2)
R(2) = RPQW(1)*MULT(2,1) + RPQW(2)*MULT(2,2)
R(3) = (RPQW(1)*MULT(3,1) + RPQW(2)*MULT(3,2))*(1.0D0/DSQRT(1.0D0
+ - ELIP2))
R(4) = DSQRT((R(1)**2.0D0) + (R(2)**2.0D0) + (R(3)**2.0D0))

WRITE(COUNT,100)R(1),R(2),R(3),R(4)

```

```

50 CONTINUE
RETURN

```

```
100 FORMAT(F12.5,5X,F12.5,5X,F12.5,5X,F12.5)
```

```
END
```

```
*
```

```

*          SUBROUTINE TWOVIS
*
* PURPOSE: This subroutine examines the visibility opportunities
*           between two satellites.
*
* VARIABLES:
* INPUT:
*   STEPS      - number of steps in the requested interval
*   SIZE       - step size (SEC)
*
* LOCAL VARIABLES:
*   COUNT      - DO loop counter
*   FILNUM    - file number
*   PHI        - angle between position vectors R1 and R2
*   R1         - position vector to satellite #1
*   R2         - position vector to satellite #2
*   VIS        - visibility function between satellites #1 and #2
*
* REFERENCES: Larson, 32
*              Alfano, Negron, and Moore, 2
*              (These references apply to THRVIS and FOURVIS also)
*****
```

### SUBROUTINE TWOVIS(STEPS,SIZE)

```

INTEGER COUNT,STEPS
REAL*8  PHI,R1(4),R2(4),SIZE,VIS
```

```

OPEN(UNIT=1,FILE='POS1.DAT',STATUS='OLD')
OPEN(UNIT=2,FILE='POS2.DAT',STATUS='OLD')
*****
```

```

* VIS.DAT CONTAINS VISIBILITY DATA BETWEEN SATELLITES ONE AND TWO
*****
```

```

OPEN(UNIT=10,FILE='VIS1.DAT',STATUS='NEW')
```

```

DO 20 COUNT = 0,STEPS
```

```

  READ(1,*)R1(1),R1(2),R1(3),R1(4)
  READ(2,*)R2(1),R2(2),R2(3),R2(4)
*****
```

```

* The next lines define the visibility function. According to this
* idea, consider a plane tangent to the earth as the line below which
* satellite to satellite visibility is not possible. The visibility
* function calculated here compares angles to determine whether the
* satellites are above or below the tangent plane. In this instance
* only two satellites are involved.
*****
```

```

* Satellites #1 and #2
*****
```

```

PHI = ((R1(1)*R2(1))+(R1(2)*R2(2))+(R1(3)*R2(3)))/(R1(4)*R2(4))
```

```

IF (PHI.GT.(1.0D0)) THEN
```

```

  PHI = 1.0D0
```

```

ELSE IF (PHI.LT.(-1.0D0)) THEN
```

```

  PHI = -1.0D0
```

```

ENDIF
```

```

VIS = (DACOS(1.0D0/R1(4)))+(DACOS(1.0D0/R2(4)))-(DACOS(PHI))
WRITE(10,110)COUNT*SIZE,VIS
```

```

20 CONTINUE
```

```

CLOSE(UNIT=1)
```

```

CLOSE(UNIT=2)
```

```

CLOSE(UNIT=10)
```

110 FORMAT(I10,5X,F12.5)

END

\*

```

*          SUBROUTINE THRVIS
*
* PURPOSE: This subroutine examines the visibility opportunities
*           between three satellites.
*
* VARIABLES:
* INPUT:
*   STEPS    - number of steps in the requested interval
*   SIZE     - step size (SEC)
*
* LOCAL VARIABLES:
*   COUNT    - DO loop counter
*   PHI      - angle between position vectors to two satellites
*   R1       - position vector to satellite #1
*   R2       - position vector to satellite #2
*   R3       - position vector to satellite #3
*   VIS      - visibility function between two satellites
*****
SUBROUTINE THRVIS(STEPS,SIZE)

INTEGER COUNT,STEPS
REAL*8 PHI,R1(4),R2(4),R3(4),SIZE,VIS

OPEN(UNIT=1,FILE='POS1.DAT',STATUS='OLD')
OPEN(UNIT=2,FILE='POS2.DAT',STATUS='OLD')
OPEN(UNIT=3,FILE='POS3.DAT',STATUS='OLD')
*****
* The following table lists filenames and their content
* UNIT = 10; VIS1.DAT - visibility between 1 and 2
* UNIT = 11; VIS2.DAT - visibility between 1 and 3
* UNIT = 12; VIS3.DAT - visibility between 2 and 3
*****
OPEN(UNIT=10,FILE='VIS1.DAT',STATUS='NEW')
OPEN(UNIT=11,FILE='VIS2.DAT',STATUS='NEW')
OPEN(UNIT=12,FILE='VIS3.DAT',STATUS='NEW')

DO 20 COUNT = 0,STEPS
    READ(1,*)R1(1),R1(2),R1(3),R1(4)
    READ(2,*)R2(1),R2(2),R2(3),R2(4)
    READ(3,*)R3(1),R3(2),R3(3),R3(4)
*****
* The following lines calculate the visibility function as explained *
* in the subroutine TWOVIS. Since three satellites are involved in *
* this case, visibility checks must be made between satellites 1 and *
* 2, 2 and 3, and 1 and 3.
*****
* Satellites #1 and #2
*****
PHI = ((R1(1)*R2(1))+(R1(2)*R2(2))+(R1(3)*R2(3)))/(R1(4)*R2(4))

IF (PHI.GT.(1.0D0)) THEN
    PHI = 1.0D0
ELSE IF (PHI.LT.(-1.0D0)) THEN
    PHI = -1.0D0
ENDIF

VIS = (DACOS(1.0D0/R1(1))) + (DACOS(1.0D0/R2(1))) - (DACOS(PHI))
WRITE(10,110)COUNT*SIZE,VIS
*****
* Satellites #1 and #3
*****
PHI = ((R1(1)*R3(1))+(R1(2)*R3(2))+(R1(3)*R3(3)))/(R1(4)*R3(4))

```

```
ELSE IF (PHI.LT.(-1.0D0)) THEN  
    PHI = -1.0D0  
ENDIF
```

```
VIS = (DACOS(1.0D0/R1(1))) + (DACOS(1.0D0/R3(1))) - (DACOS(PHI))  
WRITE(11,110)COUNT*SIZE,VIS
```

```
*****  
*      Satellites #2 and #3  
*****
```

```
PHI = ((R2(1)*R3(1))+(R2(2)*R3(2))+(R2(3)*R3(3)))/(R2(4)*R3(4))
```

```
IF (PHI.GT.(1.0D0)) THEN  
    PHI = 1.0D0  
ELSE IF (PHI.LT.(-1.0D0)) THEN  
    PHI = -1.0D0  
ENDIF
```

```
VIS = (DACOS(1.0D0/R2(4)))+(DACOS(1.0D0/R3(4)))-(DACOS(PHI))  
WRITE(12,110)COUNT*SIZE,VIS
```

```
20 CONTINUE
```

```
CLOSE(UNIT = 1)  
CLOSE(UNIT = 2)  
CLOSE(UNIT = 3)  
CLOSE(UNIT = 10)  
CLOSE(UNIT = 11)  
CLOSE(UNIT = 12)
```

```
RETURN
```

```
110 FORMAT(I10,5X,F12.5)
```

```
END
```

```
*
```

```

*          SUBROUTINE FOURVIS
*
* PURPOSE: This subroutine examines the visibility opportunities
*           between four satellites.
*
* VARIABLES:
*   INPUT:
*     STEPS - number of steps in the requested interval
*     SIZE  - step size (SEC)
*
* LOCAL VARIABLES:
*   COUNT  - DO loop counter
*   PHI    - angle between position vectors to two satellites
*   R1    - position vector to satellite #1
*   R2    - position vector to satellite #2
*   R3    - position vector to satellite #3
*   R4    - position vector to satellite #4
*   VIS   - visibility function between two satellites
*****
SUBROUTINE FOURVIS(STEPS,SIZE)

INTEGER COUNT,STEPS
REAL*8 PHI,R1(4),R2(4),R3(4),R4(4),SIZE,VIS

OPEN(UNIT=1,FILE='POS1.DAT',STATUS='OLD')
OPEN(UNIT=2,FILE='POS2.DAT',STATUS='OLD')
OPEN(UNIT=3,FILE='POS3.DAT',STATUS='OLD')
OPEN(UNIT=4,FILE='POS4.DAT',STATUS='OLD')
*****
* The following table lists filenames and their content
* UNIT = 10; VIS1.DAT - visibility between 1 and 2
* UNIT = 11; VIS2.DAT - visibility between 1 and 3
* UNIT = 12; VIS3.DAT - visibility between 1 and 4
* UNIT = 13; VIS4.DAT - visibility between 2 and 3
* UNIT = 14; VIS5.DAT - visibility between 2 and 4
* UNIT = 15; VIS6.DAT - visibility between 3 and 4
*****
OPEN(UNIT=10,FILE='VIS1.DAT',STATUS='NEW')
OPEN(UNIT=11,FILE='VIS2.DAT',STATUS='NEW')
OPEN(UNIT=12,FILE='VIS3.DAT',STATUS='NEW')
OPEN(UNIT=13,FILE='VIS4.DAT',STATUS='NEW')
OPEN(UNIT=14,FILE='VIS5.DAT',STATUS='NEW')
OPEN(UNIT=15,FILE='VIS6.DAT',STATUS='NEW')

DO 20 COUNT = 0,STEPS
  READ(1,*)R1(1),R1(2),R1(3),R1(4)
  READ(2,*)R2(1),R2(2),R2(3),R2(4)
  READ(3,*)R3(1),R3(2),R3(3),R3(4)
  READ(4,*)R4(1),R4(2),R4(3),R4(4)
*****
* The following lines calculate the visibility function as explained *
* in the subroutine TWOVIS. Since four satellites are involved in   *
* this case, visibility checks must be made between satellites 1 and *
* 2, 1 and 3, 1 and 4, 2 and 3, 2 and 4, and 3 and 4.
*****
* Satellites #1 and #2
*****
PHI = ((R1(1)*R2(1))+(R1(2)*R2(2))+(R1(3)*R2(3)))/(R1(4)*R2(4))

IF (PHI.GT.(1.0D0)) THEN
  PHI = 1.0D0
ELSE IF (PHI.LT.(-1.0D0)) THEN
  PHI = -1.0D0

```

```

***** Satellites #1 and #3 *****
* PHI = ((R1(1)*R3(1))+(R1(2)*R3(2))+(R1(3)*R3(3)))/(R1(4)*R3(4))

IF (PHI.GT.(1.0D0)) THEN
  PHI = 1.0D0
ELSE IF (PHI.LT.(-1.0D0)) THEN
  PHI = -1.0D0
ENDIF

VIS = (DACOS(1.0D0/R1(1)))+(DACOS(1.0D0/R3(1)))-(DACOS(PHI))
WRITE(11,110)COUNT*SIZE,VIS
***** Satellites #1 and #4 *****
* PHI = ((R1(1)*R4(1))+(R1(2)*R4(2))+(R1(3)*R4(3)))/(R1(4)*R4(4))

IF (PHI.GT.(1.0D0)) THEN
  PHI = 1.0D0
ELSE IF (PHI.LT.(-1.0D0)) THEN
  PHI = -1.0D0
ENDIF

VIS = (DACOS(1.0D0/R1(1)))+(DACOS(1.0D0/R4(1)))-(DACOS(PHI))
WRITE(12,110)COUNT*SIZE,VIS
***** Satellites #2 and #3 *****
* PHI = ((R2(1)*R3(1))+(R2(2)*R3(2))+(R2(3)*R3(3)))/(R2(4)*R3(4))

IF (PHI.GT.(1.0D0)) THEN
  PHI = 1.0D0
ELSE IF (PHI.LT.(-1.0D0)) THEN
  PHI = -1.0D0
ENDIF

VIS = (DACC(1.0D0/R2(1)))+(DACOS(1.0D0/R3(1)))-(DACOS(PHI))
WRITE(13,110)COUNT*SIZE,VIS
***** Satellites #2 and #4 *****
* PHI = ((R2(1)*R4(1))+(R2(2)*R4(2))+(R2(3)*R4(3)))/(R2(4)*R4(4))

IF (PHI.GT.(1.0D0)) THEN
  PHI = 1.0D0
ELSE IF (PHI.LT.(-1.0D0)) THEN
  PHI = -1.0D0
ENDIF

VIS = (DACOS(1.0D0/R2(1)))+(DACOS(1.0D0/R4(1)))-(DACOS(PHI))
WRITE(14,110)COUNT*SIZE,VIS
***** Satellites #3 and #4 *****
* PHI = ((R3(1)*R4(1))+(R3(2)*R4(2))+(R3(3)*R4(3)))/(R3(4)*R4(4))

IF (PHI.GT.(1.0D0)) THEN
  PHI = 1.0D0
ELSE IF (PHI.LT.(-1.0D0)) THEN
  PHI = -1.0D0
ENDIF

```

WRITE(15,110)COUNT\*SIZE,VIS

20 CONTINUE

CLOSE(UNIT = 1)  
CLOSE(UNIT = 2)  
CLOSE(UNIT = 3)  
CLOSE(UNIT = 4)  
CLOSE(UNIT = 10)  
CLOSE(UNIT = 11)  
CLOSE(UNIT = 12)  
CLOSE(UNIT = 13)  
CLOSE(UNIT = 14)  
CLOSE(UNIT = 15)

RETURN

110 FORMAT(I10,5X,F12.5)

END

\*

## SUBROUTINE BLEND

\* PURPOSE: The purpose of this subroutine is to parabolically blend  
 \* the points of the visibility function. The equation of  
 \* the blended curve will then be solved for real roots. If  
 \* a real root exists, it represents either a rise or set  
 \* time for the objects of interest.

## \* VARIABLES:

## \* INPUT:

\* STATE - specifies a file unit number  
 \* STEPS - number of steps  
 \* T - chronological time over time span  
 \* VIS - value of the visibility function

## \* LOCAL VARIABLES:

\* A,B - variables used in the solution of the closed form  
 \* cubic equation (Escobal, 432-434)  
 \* ALPHA - coefficients of the cubic  
 \* CHECK - slightly later time than cross. The value of check  
 \* is used to determine if a horizon crossing is a  
 \* rise or set.  
 \* COSPHI - cosine of the angle phi used in solution of the  
 \* cubic equation  
 \* COUNT - do loop counter  
 \* CROSS - time of a rise or set  
 \* D120 - 120 DEG changed to radians  
 \* D240 - 240 DEG changed to radians  
 \* DELTA - see closed form solution of cubic equation  
 \* EVENT - 1 if the crossing is a rise; 0 if the crossing is a  
 \* set  
 \* EO - see closed form solution of cubic equation  
 \* INC - increment of time T  
 \* O - coefficient of cubed variable in cubic equation  
 \* P - coefficient of squared variable in cubic equation  
 \* PHI - angle used in calculation of roots of cubic equation  
 \* PI - mathematical constant pi  
 \* Q - coefficient of the first degree variable in the  
 \* cubic equation  
 \* QTNT - portion of the quadratic equation under the radical  
 \* R - constant value in the cubic equation  
 \* ROOT1,ROOT2,ROOT3 - possible roots of the cubic equation  
 \* SINPHI - sine of the angle phi used in solution of the cubic  
 \* equation  
 \* Z1,Z2,Z3 - variables used in determining roots of the cubic  
 \* equation

\* REFERENCES: Adams and Rogers, 278-284  
 \* Alfano, Negron, and Moore, 4-5  
 \* Escobal, 431-433

\*\*\*\*\*  
SUBROUTINE BLEND(STATE,STEPS,T,VIS)

\* INTEGER COUNT,STATE,STEPS

REAL\*8 A,ARG1,ARG2,B,ALP2(0:3),ALPHA(0:3),CHECK,COSPHI,CROSS  
 REAL\*8 D120,D240,DELTA,EO,EVENT,INC,P,PHI,PI,Q,QTNT,VALA,VALB  
 REAL\*8 R,ROOT1,ROOT2,ROOT3,SINPHI,T(0:STEPS+2)  
 REAL\*8 VIS(0:STEPS+2),Z1,Z2,Z3

\*\*\*\*\*  
\* CONSTANTS

PI = DACOS(-1.0D0)

D120 = 120.0D0\*(PI/180.0D0)

\* The following lines assign values to the first and last points in \*  
\* in the visibility curve. These points fall immediately before and \*  
\* immediately after the endpoints of interest. This insures no \*  
\* portion of the curve will be emitted when testing for horizon \*  
\* crossings.

```
*****  
T(0) = T(1)  
VIS(0) = VIS(1)  
T(STEPS+1) = T(STEPS+1)  
VIS(STEPS+1) = VIS(STEPS+1)
```

\* In the following do loop, the coefficients of the cubic equation \*  
\* are determined using parabolic blending.

```
*****  
DO 10 COUNT = 1,STEPS  
    ALPHA(3) = (-.50D0)*VIS(COUNT-1)+(1.50D0)*VIS(COUNT)+(-1.50D0)*  
    + VIS(COUNT+1)+(.50D0)*VIS(COUNT+2)  
    ALPHA(2) = VIS(COUNT-1)+(-2.50D0)*VIS(COUNT)+(2.0D0)*  
    + VIS(COUNT+1)+(-.50D0)*VIS(COUNT+2)  
    ALPHA(1) = (-.50D0)*VIS(COUNT-1)+(.5D0)*VIS(COUNT+1)  
    ALPHA(0) = VIS(COUNT)
```

\* In the event that the equation is a quadratic equation instead of \*  
\* a cubic equation, the following lines determine the roots of the \*  
\* quadratic.

```
*****  
    IF (DABS(ALPHA(3)).LE.(0.000001D0).AND.DABS(ALPHA(2)).LE.  
    + (0.000001D0).AND.DABS(ALPHA(1)).LT.(.000001D0)) THEN  
        ROOT1 = -1.0D0  
        ROOT2 = -1.0D0  
        ROOT3 = -1.0D0  
        GOTO 5  
    ELSE IF (DABS(ALPHA(3)).LE.(0.000001D0).AND.DABS(ALPHA(2)).LE.  
    + (0.000001D0)) THEN  
        ROOT1 = -ALPHA(0)/ALPHA(1)  
        ROOT2 = -1.0D0  
        ROOT3 = -1.0D0  
        GOTO 5  
    ELSE IF (DABS(ALPHA(3)).LE.(0.000001D0)) THEN  
        QINT = (ALPHA(1)**2.0D0)-(1.0D0*ALPHA(2)*ALPHA(0))  
        IF (QINT.GE.(0.0D0)) THEN  
            ROOT1 = (-ALPHA(1)+DSQRT(QINT))/(2.0D0*ALPHA(2))  
            ROOT2 = (-ALPHA(1)-DSQRT(QINT))/(2.0D0*ALPHA(2))  
            ROOT3 = -1.0D0  
            GOTO 5  
        ELSE  
            ROOT1 = -1.0D0  
            ROOT2 = -1.0D0  
            ROOT3 = -1.0D0  
            GOTO 5  
        ENDIF  
    ENDIF
```

\* The following is a closed form solution to the cubic equation.. \*

```
*****  
P = ALPHA(2)/ALPHA(3)  
Q = ALPHA(1)/ALPHA(3)  
R = ALPHA(0)/ALPHA(3)  
A = (1.0D0/3.0D0)*(3.0D0*Q) - (P**2.0D0)  
B = (1.0D0/27.0D0)*((2.0D0*(P**3.0D0))-(9.0D0*P*Q)+(27.0D0*R))  
DELTA = ((A**3.0D0)/27.0D0) + ((B**2.0D0)/1.0D0)
```

```
IF (DELTA.GT./0.0D0)) THEN
```

```

    IF (ARG1.LT.(0.0D0)) THEN
        VALA = -((DABS(ARG1))**(.33333D0))
    ELSE
        VALA = ARG1**(.33333D0)
    ENDIF

    IF (ARG2.LT.(0.0D0)) THEN
        VALB = -((DABS(ARG2))**(.33333D0))
    ELSE
        VALB = ARG2**(.33333D0)
    ENDIF

    Z1 = VALA + VALB
    ROOT1 = Z1 - (P/3.0D0)
    ROOT2 = -1.0D0
    ROOT3 = -1.0D0
    ELSE IF (DELTA.EQ.(0.0D0)) THEN
        ARG1 = -B/2.0D0
        ARG2 = B/2.0D0

        IF (ARG1.LT.(0.0D0)) THEN
            Z1 = -2.0D0*((DABS(ARG1))**(.33333D0))
        ELSE IF (ARG1.GT.(0.0D0)) THEN
            Z1 = 2.0D0*((DABS(ARG1))**(.33333D0))
        ENDIF

        IF (ARG2.LT.(0.0D0)) THEN
            Z2 = -((DABS(ARG2))**(.33333D0))
        ELSE IF (ARG2.GT.(0.0D0)) THEN
            Z2 = ARG2**(.33333D0)
        ENDIF
        ROOT1 = Z1 - (P/3.0D0)
        ROOT2 = Z2 - (P/3.0D0)
        ROOT3 = -1.0D0
    ELSE IF (DELTA.LT.(0.0D0)) THEN
        ARG1 = -(A**3.0D0)/27.0D0
        ARG2 = -(A/3.0D0)

        IF (ARG1.LT.(0.0D0).OR..ARG2.LT.(0.0D0)) THEN
            ROOT1 = -1.0D0
            ROOT2 = -1.0D0
            ROOT3 = -1.0D0
        ELSE
            EO = 2.0D0*DSQRT(ARG2)
            COSPHI = -B/(2.0D0*DSQRT(ARG1))
            SINPHI = DSQRT(1.0D0-(COSPHI**2.0D0))
            PHI = DATAN2(SINPHI,COSPHI)
            Z1 = EO*DCOS(PHI/3.0D0)
            Z2 = EO*DCOS((PHI/3.0D0)+D120)
            Z3 = EO*DCOS((PHI/3.0D0)+D240)

            ROOT1 = Z1 - (P/3.0D0)
            ROOT2 = Z2 - (P/3.0D0)
            ROOT3 = Z3 - (P/3.0D0)
        ENDIF
    ENDIF
    5 CONTINUE

```

\*\*\*\*\*
\* If a positive root is found, parabolic blending is used to deter- \*
\* a cubic equation based on the times corresponding to the visibility\*
\* values of interest. The value of this cubic equation evaluated at \*
\* the root of the equation above (ROOT1,ROOT2, or ROOT3 above) to \*
\* find the exact time of crossing. The same equation is evaluated \*

```

*****
IF (ROOT1.GE.0.AND.ROOT1.LE.1) THEN
  ALP2(3) = (-.50D0)*T(COUNT-1)+(1.50D0)*T(COUNT)+(-1.50D0)*
+    T(COUNT+1)+(.50D0)*T(COUNT+2)
  ALP2(2) = T(COUNT-1)+(-2.50D0)*T(COUNT)+(2.0D0)*
+    T(COUNT+1)+(-.50D0)*T(COUNT+2)
  ALP2(1) = (-.50D0)*T(COUNT-1)+(.5D0)*T(COUNT+1)
  ALP2(0) = T(COUNT)

  CROSS = ((ROOT1**3.0D0)*ALP2(3))+((ROOT1**2.0D0)*ALP2(2))+*
+    (ROOT1*ALP2(1))+ALP2(0)
  ROOT1 = ROOT1+INC
  CHECK = ((ROOT1**3.0D0)*ALPHA(3))+((ROOT1**2.0D0)*ALPHA(2))+*
+    (ROOT1*ALPHA(1))+ALPHA(0)
  IF (CROSS.GE.(T(COUNT)).AND.CROSS.LE.(T(COUNT+1))) THEN
    IF (CHECK.GT.(0.0D0)) THEN
      WRITE(25,100)CROSS
      EVENT = 1.0D0
      WRITE(60,*)CROSS,EVENT
      WRITE(STATE,*)CROSS,EVENT
    ELSE
      WRITE(25,110)CROSS
      EVENT = 0.0D0
      WRITE(60,*)CROSS,EVENT
      WRITE(STATE,*)CROSS,EVENT
    ENDIF
  ENDIF
ENDIF

IF (ROOT2.GE.0.AND.ROOT2.LE.1) THEN
  ALP2(3) = (-.50D0)*T(COUNT-1)+(1.50D0)*T(COUNT)+(-1.50D0)*
+    T(COUNT+1)+(.50D0)*T(COUNT+2)
  ALP2(2) = T(COUNT-1)+(-2.50D0)*T(COUNT)+(2.0D0)*
+    T(COUNT+1)+(-.50D0)*T(COUNT+2)
  ALP2(1) = (-.50D0)*T(COUNT-1)+(.5D0)*T(COUNT+1)
  ALP2(0) = T(COUNT)

  CROSS = ((ROOT2**3)*ALP2(3))+((ROOT2**2)*ALP2(2))+(*
+    ALP2(1))+ALP2(0)
  ROOT2 = ROOT2+INC
  CHECK = ((ROOT2**3)*ALPHA(3))+((ROOT2**2)*ALPHA(2))+(*
+    ALPHA(1))+ALPHA(0)
  IF (CROSS.GE.(T(COUNT)).AND.CROSS.LE.(T(COUNT+1))) THEN
    IF (CHECK.GT.(0.0D0)) THEN
      WRITE(25,100)CROSS
      EVENT = 1.0D0
      WRITE(60,*)CROSS,EVENT
      WRITE(STATE,*)CROSS,EVENT
    ELSE
      WRITE(25,110)CROSS
      EVENT = 0.0D0
      WRITE(60,*)CROSS,EVENT
      WRITE(STATE,*)CROSS,EVENT
    ENDIF
  ENDIF
ENDIF

IF (ROOT3.GE.0.AND.ROOT3.LE.1) THEN
  ALP2(3) = (-.50D0)*T(COUNT-1)+(1.50D0)*T(COUNT)+(-1.50D0)*
+    T(COUNT+1)+(.50D0)*T(COUNT+2)
  ALP2(2) = T(COUNT-1)+(-2.50D0)*T(COUNT)+(2.0D0)*
+    T(COUNT+1)+(-.50D0)*T(COUNT+2)
  ALP2(1) = (-.50D0)*T(COUNT-1)+(.5D0)*T(COUNT+1)

```

```
+ -----  
+ ALP2(1))+ALP2(0)  
ROOT3 = ROOT3+INC  
CHECK = ((ROOT3**3)*ALPHA(3))+((ROOT3**2)*ALPHA(2))+(ROOT3*  
+ ALPHA(1))+ALPHA(0)  
IF (CROSS.GE.(T(COUNT)).AND.CROSS.LE.(T(COUNT+1))) THEN  
IF (CHECK.GT.(0.0D0)) THEN  
WRITE(25,100)CROSS  
EVENT = 1.0D0  
WRITE(60,*)CROSS,EVENT  
WRITE(STATE,*)CROSS,EVENT  
ELSE  
WRITE(25,110)CROSS  
EVENT = 0.0D0  
WRITE(60,*)CROSS,EVENT  
WRITE(STATE,*)CROSS,EVENT  
ENDIF  
ENDIF  
ENDIF
```

10 CONTINUE

```
100 FORMAT(F12.5,' SEC - RISE')  
110 FORMAT(F12.5,' SEC - SET')
```

```
RETURN  
END
```

\*

```

*          SUBROUTINE GSSCVC1
*
* PURPOSE: The purpose of this subroutine is to accomplish a
*           check for constant visibility between a ground station
*           and 2 satellites.
*
* VARIABLES:
*   INPUT:
*     STATE - File number specifier
*
* LOCAL VARIABLES:
*   CHANGE - specifies when communication is broken or re-
*             established
*   COUNT - do loop counter
*   E1,E2 - Specifies rise/set time for visibility function
*             a ground station and 2 satellites
*   EVENT - Array of all rise/set times
*   IN - do loop counter
*   RS1,RS2 - 1 if the event is a rise; 0 if the event is a set
*   SUM - Sum of RS1 and RS2 at a given event
*   T - time zero of any selected visibility function
*             - in this subroutine T is a place holder
*   TEMP - Temporary value used in sort loop
*   TOTAL - Total number of events
*   TOT1 - Number of events between Ground Station #? and
*             Satellite #1
*   TOT2 - Number of events between Ground Station #? and
*             Satellite #2
*   TT - Holds all event times and the corresponding
*             status of the visibility function for each
*             viewing path
*   V - the first value of the selected visibility
*             function
*   X - do loop counter
*****

```

#### SUBROUTINE GSSCVC1(STATE)

```

REAL*8 E1(0:100),E2(0:100),EVENT(0:500)
REAL*8 RS1(0:100),RS2(0:100),SUM,T,TEMP,TT(0:500,2),V
INTEGER COUNT,CHANGE,CHECK,IN,STATE,TOTAL,TOT1,TOT2,X

```

```

OPEN(UNIT=41,FILE='STAT1.DAT',STATUS='OLD')
OPEN(UNIT=42,FILE='STAT2.DAT',STATUS='OLD')
OPEN(UNIT=60,FILE='TRACKER.DAT',STATUS='OLD')

```

```

REWIND(UNIT=60)

```

```

OPEN(UNIT=10,FILE='VIS1.DAT',STATUS='OLD')
OPEN(UNIT=11,FILE='VIS2.DAT',STATUS='OLD')

```

```

WRITE(*,*)"The computer is in the process of determining whether"
WRITE(*,*)"or not continuous communications is possible. When "
WRITE(*,*)"the program is finished running results can be found"
WRITE(*,*)"in the file RISESET.DAT."

```

```

*****
*          GROUND STATION AND SATELLITE #1
*****

```

```

TOT1 = 0
DO 20 COUNT = 1,100
READ(STATE,*END=25)E1(COUNT),RS1(COUNT)
TOT1 = COUNT

```

20 CONTINUE

```

READ(10,*)T,V
IF (V.GT.(0.0D0)) THEN
    RS1(0) = 1.0D0
ELSE
    RS1(0) = 0.0D0
ENDIF
ELSE IF (RS1(1).EQ.(0.0D0)) THEN
    RS1(0) = 1.0D0
ELSE
    RS1(0) = 0.0D0
ENDIF
*****
* GROUND STATION AND SATELLITE #2 *
*****
TOT2 = 0
DO 30 COUNT = 1,100
    READ(STATE+1,*,END=35)E2(COUNT),RS2(COUNT)
    TOT2 = COUNT
30 CONTINUE
35 E2(0) = 0.0D0

IF (TOT2.EQ.0) THEN
    READ(11,*)T,V
    IF (V.GT.(0.0D0)) THEN
        RS2(0) = 1.0D0
    ELSE
        RS2(0) = 0.0D0
    ENDIF
    ELSE IF (RS2(1).EQ.(0.0D0)) THEN
        RS2(0) = 1.0D0
    ELSE
        RS2(0) = 0.0D0
    ENDIF
*****
* The following calculates the total number of events between the *
* ground station and two satellites. *
*****
TOTAL = TOT1+TOT2

CHECK = 0
DO 45 COUNT = 1,500
    READ(60,*,END=48)EVENT(COUNT)
    CHECK = COUNT
45 CONTINUE
48 CONTINUE

IF (CHECK.EQ.0) THEN
    WRITE(25,*)"There were no visibility opportunities with this
+ configuration."
    GOTO 140
ENDIF
*****
* The following orders all the events from the smallest to the *
* largest. *
*****
DO 60 COUNT = 1,TOTAL-1
    DO 50 X = 1,TOTAL-1
        IF (EVENT(X+1).LT.EVENT(X)) THEN
            TEMP      = EVENT(X+1)
            EVENT(X+1) = EVENT(X)
            EVENT(X)   = TEMP
        ENDIF
50 CONTINUE
60 CONTINUE

```

```

*****
* The following determines the status of communications for each *
* possible visibility path at each event. *
*****
DO 80 COUNT = 0,TOTAL
  IF (TOT1.EQ.0) THEN
    TT(COUNT,1) = RS1(0)
    GOTO 80
  ENDIF
  DO 70 IN = 0,TOT1 - 1
    IF (EVENT(COUNT).GE.E1(IN).AND.EVENT(COUNT).LT.E1(IN+1)) THEN
      TT(COUNT,1) = RS1(IN)
      GOTO 80
    ELSE IF (EVENT(COUNT).EQ.E1(IN+1)) THEN
      TT(COUNT,1) = RS1(IN+1)
      GOTO 80
    ELSE IF (EVENT(COUNT).GT.E1(IN+1).AND.IN.EQ.(TOT1-1)) THEN
      TT(COUNT,1) = RS1(IN+1)
      GOTO 80
    ENDIF
  70 CONTINUE
  80 CONTINUE

  DO 120 COUNT = 0,TOTAL
    IF (TOT2.EQ.0) THEN
      TT(COUNT,2) = RS2(0)
      GOTO 120
    ENDIF
    DO 110 IN = 0,TOT2 - 1
      IF (EVENT(COUNT).GE.E2(IN).AND.EVENT(COUNT).LT.E2(IN+1)) THEN
        TT(COUNT,2) = RS2(IN)
        GOTO 120
      ELSE IF (EVENT(COUNT).EQ.E2(IN+1)) THEN
        TT(COUNT,2) = RS2(IN+1)
        GOTO 120
      ELSE IF (EVENT(COUNT).GT.E2(IN+1).AND.IN.EQ.(TOT2-1)) THEN
        TT(COUNT,2) = RS2(IN+1)
        GOTO 120
      ENDIF
    110 CONTINUE
    120 CONTINUE

    CHANGE = 1
*****
* The next DO loop determines if constant communication is *
* possible. If the sum is equal to zero, communication is not *
* possible. If the sum is greater than or equal to one, communi- *
* cation is possible. *
*****
DO 130 COUNT = 0,TOTAL
  SUM = TT(COUNT,1) + TT(COUNT,2)
  IF (SUM.EQ.(0.0D0).AND.CHANGE.EQ.1) THEN
    WRITE(25,*)'Communications broken at ',EVENT(COUNT)
    CHANGE = 0
  ENDIF

  IF (SUM.GE.(1.0D0).AND.CHANGE.EQ.0) THEN
    WRITE(25,*)'Communications re-established at ',EVENT(COUNT)
    CHANGE = 1
  ENDIF
  130 CONTINUE
  140 CONTINUE

```

CLOSE(UNIT=10,STATUS='DELETE')  
CLOSE(UNIT=11,STATUS='DELETE')

RETURN  
END

\*

```

***** **** SUBROUTINE CVC3 ****
*
* PURPOSE: The purpose of this subroutine is to accomplish a
* check for constant visibility between 3 satellites.
* For visibility to be maintained, at least two
* paths of visibility must be maintained at all times.
*
* VARIABLES:
* INPUT:
*   KIND      - specifies whether 3 satellites are involved (1)
*                 or a ground station and 3 satellites are
*                 involved (0)
*   STATE     - File number specifier
*
* LOCAL VARIABLES:
*   CHANGE    - specifies when communication is broken or re-
*                 established
*   COUNT     - do loop counter
*   E1...,E3  - Specifies rise/set time for visibility function
*                 between 3 satellites or a ground station and
*                 3 satellites
*   EVENT     - Array of all rise/set times
*   IN        - do loop counter
*   RS1...,RS3 - 1 if the event is a rise; 0 if the event is a set
*   SUM       - Sum of RS1...,RS3 at a given event
*   T          - time zero read from file of visibility data
*                 - in this subroutine, T serves only as a place
*                   holder
*   TEMP      - Temporary value used in sort loop
*   TOTAL     - Total number of events
*   TOT1      - Number of events between Satellite #1 and
*                 Satellite #2 or Ground Station #? and
*                 Satellite #1
*   TOT2      - Number of events between Satellite #2 and
*                 Satellite #3 or Ground Station #? and
*                 Satellite #2
*   TOT3      - Number of events between Satellite #1 and
*                 Satellite #3 or Ground Station #? and
*                 Satellite #3
*   TT        - Holds all event times and the corresponding
*                 status of the visibility function for each
*                 viewing path
*   V         - value of the chosen visibility function at time
*                 equal to zero
*   X         - do loop counter
*****

```

#### SUBROUTINE CVC3(KIND,STATE)

```

REAL*8 E1(0:100),E2(0:100),E3(0:100),EVENT(0:500),RS1(0:100)
REAL*8 RS2(0:100),RS3(0:100),SUM,T,TEMP,TT(0:500,3),V
INTEGER CHANGE,COUNT,IN,KIND,STATE,TOTAL,TOT1,TOT2,TOT3,X

```

```

IF (KIND.EQ.1) THEN
  WRITE(*,*) ''
  WRITE(*,*)"The computer is in the process of determining"
  WRITE(*,*)"whether or not constant communications is"
  WRITE(*,*)"maintained. When the program has finished"
  WRITE(*,*)"running, results may be found in RISESET.DAT."
ENDIF

```

```

OPEN(UNIT=41,FILE='STAT1.DAT',STATUS='OLD')

```

```
OPEN(UNIT=60,FILE='TRACKER.DAT',STATUS='OLD')

IF (KIND.EQ.0) THEN
    REWIND(UNIT=60)
ENDIF

OPEN(UNIT=10,FILE='VIS1.DAT',STATUS='OLD')
OPEN(UNIT=11,FILE='VIS2.DAT',STATUS='OLD')
OPEN(UNIT=12,FILE='VIS3.DAT',STATUS='OLD')
*****
* The following DO loops read the rise and set times for each vis-
* ibility path.
*****
*          SATELLITE #1 AND SATELLITE #2
*          GROUND STATION AND SATELLITE #1
*****
TOT1 = 0
DO 20 COUNT = 1,100
    READ(STATE,*,END=25)E1(COUNT),RS1(COUNT)
    TOT1 = COUNT
20 CONTINUE
25 E1(0) = 0.0D0
*****
* If there were no rise or set times, the file containing the vis-
* ibility data must be referenced to determine if the two objects
* of interest are always in view or never in view.
*****
IF (TOT1.EQ.0) THEN
    READ(10,*)T,V
    IF (V.GT.(0.0D0)) THEN
        RS1(0)=1.0D0
    ELSE
        RS1(0)=0.0D0
    ENDIF
*****
* The following line checks the first condition of the first rise
* or set time then assigns the appropriate condition to time zero.
*****
    ELSE IF (RS1(1).EQ.(0.0D0)) THEN
        RS1(0) = 1.0D0
    ELSE
        RS1(0) = 0.0D0
    ENDIF
*****
*          SATELLITE #1 AND SATELLITE #3
*          GROUND STATION AND SATELLITE #2
*****
TOT2 = 0
DO 30 COUNT = 1,100
    READ(STATE+1,*,END=35)E2(COUNT),RS2(COUNT)
    TOT2 = COUNT
30 CONTINUE
35 E2(0) = 0.0D0

IF (TOT2.EQ.0) THEN
    READ(11,*)T,V
    IF (V.GT.(0.0D0)) THEN
        RS2(0)=1.0D0
    ELSE
        RS2(0)=0.0D0
    ENDIF
*****
* The following line checks the first condition of the first rise
* or set time then assigns the appropriate condition to time zero.
*****
```

```

RS2(0) = 1.0D0
ELSE
  RS2(0) = 0.0D0
ENDIF
*****
*      SATELLITE #2 AND SATELLITE #3
*      GROUND STATION AND SATELLITE #3
*****
TOT3 = 0
DO 40 COUNT = 1,100
  READ(STATE+2,*,END=45)E3(COUNT),RS?(COUNT)
  TOT3 = COUNT
40 CONTINUE
45 E3(0) = 0.0D0

IF (TOT3.EQ.0) THEN
  READ(12,*)T,V
  IF (V.GT.(0.0D0)) THEN
    RS3(0)=1.0D0
  ELSE
    RS3(0)=0.0D0
  ENDIF
*****
* The following line checks the first condition of the first rise *
* or set time then assigns the appropriate condition to time zero. *
*****
ELSE IF (RS3(1).EQ.(0.0D0)) THEN
  RS3(0) = 1.0D0
ELSE
  RS3(0) = 0.0D0
ENDIF
*****
* The following calculates the total number of rise/set events   *
* between the ground station and the three satellites or between   *
* the three satellites.                                         *
*****
TOTAL = TOT1+TOT2+TOT3

DO 47 COUNT = 1,500
  READ(60,*,END=48)EVENT(COUNT)
47 CONTINUE
48 CONTINUE
*****
* If there were no rise/set times at all, the following message is *
* written to the final output file and the program ends.           *
*****
' IF (COUNT.EQ.1) THEN
  WRITE(25,*)"There were no opportunities for viewing
  + with this configuration."
  GOTO 215
ENDIF
*****
* The following performs a sort to place the list of all events in *
* order from smallest number to largest.                            *
*****
DO 60 COUNT = 1,TOTAL-1
  DO 50 X = 1,TOTAL-1
    IF (EVENT(X+1).LT.EVENT(X)) THEN
      TEMP = EVENT(X+1)
      EVENT(X+1) = EVENT(X)
      EVENT(X) = TEMP
    ENDIF
  50 CONTINUE
60 CONTINUE

```

\*\*\*\*\*  
\* The following loops determine the intermediate status of v\*,ibil-\*  
\* ity at each event.  
\*\*\*\*\*

```
DO 80 COUNT = 0,TOTAL
  IF (TOT1.EQ.0) THEN
    TT(COUNT,1) = RS1(0)
    GOTO 80
  ENDIF
  DO 70 IN = 0,TOT1 - 1
    IF (EVENT(COUNT).GE.E1(IN).AND.EVENT(COUNT).LT.E1(IN+1)) THEN
      TT(COUNT,1) = RS1(IN)
      GOTO 80
    ELSE IF (EVENT(COUNT).EQ.E1(IN+1)) THEN
      TT(COUNT,1) = RS1(IN+1)
      GOTO 80
    ELSE IF (EVENT(COUNT).GT.E1(IN+1).AND.IN.EQ.(TOT1-1)) THEN
      TT(COUNT,1) = RS1(TOT1)
      GOTO 80
    ENDIF
  70 CONTINUE
  80 CONTINUE

  DO 100 COUNT = 0,TOTAL
    IF (TOT2.EQ.0) THEN
      TT(COUNT,2) = RS2(0)
      GOTO 100
    ENDIF
    DO 90 IN = 0,TOT2 - 1
      IF (EVENT(COUNT).GE.E2(IN).AND.EVENT(COUNT).LT.E2(IN+1)) THEN
        TT(COUNT,2) = RS2(IN)
        GOTO 100
      ELSE IF (EVENT(COUNT).EQ.E2(IN+1)) THEN
        TT(COUNT,2) = RS2(IN+1)
        GOTO 100
      ELSE IF (EVENT(COUNT).GT.E2(IN+1).AND.IN.EQ.(TOT2-1)) THEN
        TT(COUNT,2) = RS2(TOT2)
        GOTO 100
      ENDIF
    90 CONTINUE
    100 CONTINUE

    DO 120 COUNT = 0,TOTAL
    DO 110 IN = 0,TOT3 - 1
      IF (EVENT(COUNT).GE.E3(IN).AND.EVENT(COUNT).LT.E3(IN+1)) THEN
        TT(COUNT,3) = RS3(IN)
        GOTO 120
      ELSE IF (EVENT(COUNT).EQ.E3(IN+1)) THEN
        TT(COUNT,3) = RS3(IN+1)
        GOTO 120
      ELSE IF (EVENT(COUNT).GT.E3(IN+1).AND.IN.EQ.(TOT3-1)) THEN
        TT(COUNT,3) = RS3(TOT3)
        GOTO 120
      ENDIF
    110 CONTINUE
    120 CONTINUE
```

CHANGE = 1

\*\*\*\*\*  
\* The following determines if continuous communication is possible.\*  
\* For 3 satellites, the sum must be greater than or equal to 2. \*  
\* For a ground station and three satellites, the sum must be \*  
\* greater than or equal to 1. \*

IF (KIND.EQ.1) THEN

```
IF (SUM.LE.(1.0D0).AND.CHANGE.EQ.1) THEN
  WRITE(25,200)EVENT(COUNT)
  CHANGE = 0
ENDIF

IF (SUM.GE.(2.0D0).AND.CHANGE.EQ.0) THEN
  WRITE(25,210)EVENT(COUNT)
  CHANGE = 1
ENDIF
130 CONTINUE

ELSE IF (KIND.EQ.0) THEN
  DO 140 COUNT = 0,TOTAL
    SUM = TT(COUNT,1) + TT(COUNT,2) + TT(COUNT,3)
    IF (SUM.LT.(1.0D0).AND.CHANGE.EQ.1) THEN
      WRITE(25,200)EVENT(COUNT)
      CHANGE = 0
    ENDIF

    IF (SUM.GE.(1.0D0).AND.CHANGE.EQ.0) THEN
      WRITE(25,210)EVENT(COUNT)
      CHANGE = 1
    ENDIF
  140 CONTINUE
ENDIF

215 CONTINUE

CLOSE(UNIT=STATE,STATUS='DELETE')
CLOSE(UNIT=STATE+1,STATUS='DELETE')
CLOSE(UNIT=STATE+2,STATUS='DELETE')
CLOSE(UNIT=60)
CLOSE(UNIT=10,STATUS='DELETE')
CLOSE(UNIT=11,STATUS='DELETE')
CLOSE(UNIT=12,STATUS='DELETE')

200 FORMAT('Communications broken at ',F12.5,' SEC')
210 FORMAT('Communications re-established at ',F12.5,' SEC')

RETURN
END
```

```

*          SUBROUTINE CVC4
*
* PURPOSE: The purpose of this subroutine is to accomplish a
*           check for constant visibility between 4 satellites.
*           For visibility to be maintained, at least 3
*           paths of visibility must be maintained at all times.
*
* VARIABLES:
*   INPUT:
*     STATE - File number specifier
*
* LOCAL VARIABLES:
*   CHANGE - specifies when communication is broken or re-
*             established
*   COUNT - do loop counter
*   E1,...,E6 - Specifies rise/set time for visibility function
*               between 6 satellites
*   EVENT - Array of all rise/set times
*   IN - do loop counter
*   RS1...RS6 - 1 if the event is a rise; 0 if the event is a set
*   SUM - Sum of RS1...RS6 at a given event
*   T - time zero read from file of visibility data
*       - in this subroutine, T serves only as a place
*         holder
*   TEMP - Temporary value used in sort loop
*   TOTAL - Total number of events
*   TOT1 - Number of events between Satellite #1 and
*          Satellite #2
*   TOT2 - Number of events between Satellite #1 and
*          Satellite #3
*   TOT3 - Number of events between Satellite #1 and
*          Satellite #4
*   TOT4 - Number of events between Satellite #2 and
*          Satellite #3
*   TOT5 - Number of events between Satellite #2 and
*          Satellite #4
*   TOT6 - Number of events between Satellite #3 and
*          Satellite #4
*   TT - Holds all event times and the corresponding
*        status of the visibility function for each
*        viewing path
*   V - value of the chosen visibility function at time
*      equal to zero
*   X - do loop counter

```

SUBROUTINE CVC4(STATE)

```

REAL*8 E1(0:50),E2(0:50),E3(0:50),E4(0:50),E5(0:50)
REAL*8 E6(0:50),EVENT(0:200),RS1(0:50),RS2(0:50),RS3(0:50)
REAL*8 RS4(0:50),RS5(0:50),RS6(0:50),SUM,T,TEMP,TT(0:200,6),V
INTEGER CHANGE,COUNT,IN,STATE,TOTAL,TOT1,TOT2,TOT3,TOT4,TOT5
INTEGER TOT6,X

```

```

WRITE(*,*)
WRITE(*,*)'The computer is in the process of determining'
WRITE(*,*)'whether or not constant communications is'
WRITE(*,*)'maintained. When the program has finished'
WRITE(*,*)'running, results may be found in RISESET.DAT.'

```

```

OPEN(UNIT=41,FILE='STAT1.DAT',STATUS='OLD')
OPEN(UNIT=42,FILE='STAT2.DAT',STATUS='OLD')
OPEN(UNIT=43,FILE='STAT3.DAT',STATUS='OLD')
OPEN(UNIT=44,FILE='STAT4.DAT',STATUS='OLD')

```

```
OPEN(UNIT=10,FILE='VIS1.DAT',STATUS='OLD')
OPEN(UNIT=11,FILE='VIS2.DAT',STATUS='OLD')
OPEN(UNIT=12,FILE='VIS3.DAT',STATUS='OLD')
OPEN(UNIT=13,FILE='VIS4.DAT',STATUS='OLD')
OPEN(UNIT=14,FILE='VIS5.DAT',STATUS='OLD')
OPEN(UNIT=15,FILE='VIS6.DAT',STATUS='OLD')
*****
*          SATELLITE #1 AND SATELLITE #2
*****
TOT1 = 0
DO 20 COUNT = 1,100
    READ(STATE,*,"END=25")E1(COUNT),RS1(COUNT)
    TOT1 = COUNT
20 CONTINUE
25 E1(0) = 0.0D0

    IF (TOT1.EQ.0) THEN
        READ(10,*)T,V
        IF (V.GT.(0.0D0)) THEN
            RS1(0)=1.0D0
        ELSE
            RS1(0)=0.0D0
        ENDIF
    ELSE IF (RS1(1).EQ.(0.0D0)) THEN
        RS1(0) = 1.0D0
    ELSE
        RS1(0) = 0.0D0
    ENDIF
*****
*          SATELLITE =1 AND SATELLITE =3
*****
TOT2 = 0
DO 30 COUNT = 1,100
    READ(STATE+1,*,"END=35")E2(COUNT),RS2(COUNT)
    TOT2 = COUNT
30 CONTINUE
35 E2(0) = 0.0D0

    IF (TOT2.EQ.0) THEN
        READ(11,*)T,V
        IF (V.GT.(0.0D0)) THEN
            RS2(0)=1.0D0
        ELSE
            RS2(0)=0.0D0
        ENDIF
    ELSE IF (RS2(1).EQ.(0.0D0)) THEN
        RS2(0) = 1.0D0
    ELSE
        RS2(0) = 0.0D0
    ENDIF
*****
*          SATELLITE #1 AND SATELLITE #4
*****
TOT3 = 0
DO 40 COUNT = 1,100
    READ(STATE+2,*,"END=45")E3(COUNT),RS3(COUNT)
    TOT3 = COUNT
40 CONTINUE
45 E3(0) = 0.0D0

    IF (TOT3.EQ.0) THEN
        READ(12,*)T,V
```

```

        ENDIF
*****
* The following line checks the first condition of the first rise *
* or set time then assigns the appropriate condition to time zero. *
*****
        ELSE IF (RS3(1).EQ.(0.0D0)) THEN
            RS3(0) = 1.0D0
        ELSE
            RS3(0) = 0.0D0
        ENDIF
*****
*          SATELLITE #2 AND SATELLITE #3
*****
        TOT4 = 0
        DO 50 COUNT = 1,100
            READ(STATE+3,*END=55)E4(COUNT),RS4(COUNT)
            TOT4 = COUNT
50 CONTINUE
55 E4(0) = 0.0D0

        IF (TOT4.EQ.0) THEN
            READ(13,*)T,V
            IF (V.GT.(0.0D0)) THEN
                RS4(0)=1.0D0
            ELSE
                RS4(0)=0.0D0
            ENDIF
*****
* The following line checks the first condition of the first rise *
* or set time then assigns the appropriate condition to time zero. *
*****
        ELSE IF (RS4(1).EQ.(0.0D0)) THEN
            RS4(0) = 1.0D0
        ELSE
            RS4(0) = 0.0D0
        ENDIF
*****
*          SATELLITE #2 AND SATELLITE #4
*****
        TOT5 = 0
        DO 60 COUNT = 1,100
            READ(STATE+4,*END=65)E5(COUNT),RS5(COUNT)
            TOT5 = COUNT
60 CONTINUE
65 E5(0) = 0.0D0

        IF (TOT5.EQ.0) THEN
            READ(14,*)T,V
            IF (V.GT.(0.0D0)) THEN
                RS5(0)=1.0D0
            ELSE
                RS5(0)=0.0D0
            ENDIF
*****
* The following line checks the first condition of the first rise *
* or set time then assigns the appropriate condition to time zero. *
*****
        ELSE IF (RS5(1).EQ.(0.0D0)) THEN
            RS5(0) = 1.0D0
        ELSE
            RS5(0) = 0.0D0
        ENDIF

```

```

**** -
DO 70 COUNT = 1,100
READ(STATE+5,*,END=73)E6(COUNT),RS6(COUNT)
TOT6 = COUNT
70 CONTINUE
73 E6(0) = 0.000

IF (TOT6.EQ.0) THEN
READ(15,*)T,V
IF (V.GT.(0.000)) THEN
RS6(0)=1.000
ELSE
RS6(0)=0.000
ENDIF
*****
* The following line checks the first condition of the first rise *
* or set time then assigns the appropriate condition to time zero. *
*****
ELSE IF (RS6(1).EQ.(0.000)) THEN
RS6(0) = 1.000
ELSE
RS6(0) = 0.000
ENDIF
*****
* The following calculates the total number of rise/set events *
* between the ground station and the three satellites. *
*****
TOTAL = TOT1+TOT2+TOT3+TOT4+TOT5+TOT6

DO 75 COUNT = 1,500
READ(60,*,END=76)EVENT(COUNT)
75 CONTINUE
76 CONTINUE
*****
* If there were no rise/set times at all, the following message is *
* written to the final output file and the program ends. *
*****
IF (COUNT.EQ.1) THEN
WRITE(25,*)"There were no opportunities for viewing with this
+ configuration."
GOTO 215
ENDIF
*****
* The following performs a sort to place the list of all events in *
* order from smallest number to largest. *
*****
DO 80 COUNT = 1,TOTAL-1
DO 78 X = 1,TOTAL-1
IF (EVENT(X+1).LT.EVENT(X)) THEN
TEMP = EVENT(X+1)
EVENT(X+1) = EVENT(X)
EVENT(X) = TEMP
ENDIF
78 CONTINUE
80 CONTINUE

EVENT(0) = 0.000
*****
* The following loops determine the intermediate status of visibility at each event.
*****
DO 100 COUNT = 0,TOTAL
IF (TOT1.EQ.0) THEN

```

```

    TT(COUNT,1) = RS1(IN)
    GOTO 100
ELSE IF (EVENT(COUNT).EQ.E1(IN+1)) THEN
    TT(COUNT,1) = RS1(IN+1)
    GOTO 100
ELSE IF (EVENT(COUNT).GT.E1(IN).AND.IN.EQ.(TOT1-1)) THEN
    TT(COUNT,1) = RS1(TOT1)
    GOTO 100
ENDIF
90 CONTINUE
100 CONTINUE

DO 120 COUNT = 0,TOTAL
    IF (TOT2.EQ.0) THEN
        TT(COUNT,2) = RS2(0)
        GOTO 120
    ENDIF
DO 110 IN = 0,TOT2 - 1
    IF (EVENT(COUNT).GE.E2(IN).AND.EVENT(COUNT).LT.E2(IN+1)) THEN
        TT(COUNT,2) = RS2(IN)
        GOTO 120
    ELSE IF (EVENT(COUNT).EQ.E2(IN+1)) THEN
        TT(COUNT,2) = RS2(IN+1)
        GOTO 120
    ELSE IF (EVENT(COUNT).GT.E2(IN).AND.IN.EQ.(TOT2-1)) THEN
        TT(COUNT,2) = RS2(TOT2)
        GOTO 120
    ENDIF
110 CONTINUE
120 CONTINUE

DO 140 COUNT = 0,TOTAL
    IF (TOT3.EQ.0) THEN
        TT(COUNT,3) = RS3(0)
        GOTO 140
    ENDIF
DO 130 IN = 0,TOT3 - 1
    IF (EVENT(COUNT).GE.E3(IN).AND.EVENT(COUNT).LT.E3(IN+1)) THEN
        TT(COUNT,3) = RS3(IN)
        GOTO 140
    ELSE IF (EVENT(COUNT).EQ.E3(IN+1)) THEN
        TT(COUNT,3) = RS3(IN+1)
        GOTO 140
    ELSE IF (EVENT(COUNT).GT.E3(IN).AND.IN.EQ.(TOT3-1)) THEN
        TT(COUNT,3) = RS3(TOT3)
        GOTO 140
    ENDIF
130 CONTINUE
140 CONTINUE

DO 160 COUNT = 0,TOTAL
    IF (TOT4.EQ.0) THEN
        TT(COUNT,4) = RS4(0)
        GOTO 160
    ENDIF
DO 150 IN = 0,TOT4 - 1
    IF (EVENT(COUNT).GE.E4(IN).AND.EVENT(COUNT).LT.E4(IN+1)) THEN
        TT(COUNT,4) = RS4(IN)
        GOTO 160
    ELSE IF (EVENT(COUNT).EQ.E4(IN+1)) THEN
        TT(COUNT,4) = RS4(IN+1)

```

160 CONTINUE

```
DO 180 COUNT = 0, TOTAL
  IF (TOT5.EQ.0) THEN
    TT(COUNT,5) = RS5(0)
    GOTO 180
  ENDIF
  DO 170 IN = 0, TOT5 - 1
  IF (EVENT(COUNT).GE.E5(IN).AND.EVENT(COUNT).LT.E5(IN+1)) THEN
    TT(COUNT,5) = RS5(IN)
    GOTO 180
  ELSE IF (EVENT(COUNT).EQ.E5(IN+1)) THEN
    TT(COUNT,5) = RS5(IN+1)
    GOTO 180
  ELSE IF (EVENT(COUNT).GT.E5(IN).AND.IN.EQ.(TOT5-1)) THEN
    TT(COUNT,5) = RS5(TOT5)
    GOTO 180
  ENDIF
```

170 CONTINUE
180 CONTINUE

```
DO 200 COUNT = 0, TOTAL
  IF (TOT6.EQ.0) THEN
    TT(COUNT,6) = RS6(0)
    GOTO 200
  ENDIF
  DO 190 IN = 0, TOT6 - 1
  IF (EVENT(COUNT).GE.E6(IN).AND.EVENT(COUNT).LT.E6(IN+1)) THEN
    TT(COUNT,6) = RS6(IN)
    GOTO 200
  ELSE IF (EVENT(COUNT).EQ.E6(IN+1)) THEN
    TT(COUNT,6) = RS6(IN+1)
    GOTO 200
  ELSE IF (EVENT(COUNT).GT.E6(IN).AND.IN.EQ.(TOT6-1)) THEN
    TT(COUNT,6) = RS6(TOT6)
    GOTO 200
  ENDIF
```

190 CONTINUE
200 CONTINUE

CHANGE = 1

\*\*\*\*\*  
\* The following determines if continuous communication is possible.\*  
\* For 4 satellites, the sum must be greater than or equal to 3. \*  
\*\*\*\*\*

```
DO 210 COUNT = 0, TOTAL
  SUM = TT(COUNT,1) + TT(COUNT,2) + TT(COUNT,3) + TT(COUNT,4) +
        + TT(COUNT,5) + TT(COUNT,6)
  IF (SUM.LT.(3.0D0).AND.CHANGE.EQ.1) THEN
    WRITE(25,220) EVENT(COUNT)
    CHANGE = 0
  ENDIF

  IF (SUM.GE.(3.0D0).AND.CHANGE.EQ.0) THEN
    WRITE(25,230) EVENT(COUNT)
    CHANGE = 1
  ENDIF
```

210 CONTINUE
215 CONTINUE

```
CLOSE(UNIT=STATE+5,STATUS='DELETE')
CLOSE(UNIT=60)
```

```
CLOSE(UNIT=10,STATUS='DELETE')
CLOSE(UNIT=11,STATUS='DELETE')
CLOSE(UNIT=12,STATUS='DELETE')
CLOSE(UNIT=13,STATUS='DELETE')
CLOSE(UNIT=14,STATUS='DELETE')
CLOSE(UNIT=15,STATUS='DELETE')
```

```
220 FORMAT('Communications broken at ',F12.5,' SEC')
230 FORMAT('Communications re-established at ',F12.5,' SEC')
```

```
RETURN
END
```

```

*****
*          SUBROUTINE GSSCVC4
* (Ground Station Satellite Continuous Visibility Check (4))
* PURPOSE: The purpose of this subroutine is to accomplish a
* check for constant visibility between a ground station
* and 3 satellites.
*
* VARIABLES:
* INPUT:
* STATE      - File number specifier
*
* LOCAL VARIABLES:
* CHANGE     - specifies when communication is broken or re-
*               established
* COUNT      - do loop counter
* E1,...,E4   - Specifies rise/set time for visibility function
*               a ground station and 4 satellites
* EVENT      - Array of all rise/set times
* IN         - do loop counter
* RS1,..,RS4 - 1 if the event is a rise; 0 if the event is a set
* SUM        - Sum of RS1,..,RS4 at a given event
* T          - time zero of any selected visibility function
*               - in this subroutine T is a place holder
* TEMP       - Temporary value used in sort loop
* TOTAL      - Total number of events
* TOT1       - Number of events between Ground Station #? and
*               Satellite #1
* TOT2       - Number of events between Ground Station #? and
*               Satellite #2
* TOT3       - Number of events between Ground Station #? and
*               Satellite #3
* TOT4       - Number of events between Ground Station #? and
*               Satellite #4
* TT         - Holds all event times and the corresponding
*               status of the visibility function for each
*               viewing path
* V          - the first value of the selected visibility
*               function
* X          - do loop counter
*****

```

#### SUBROUTINE GSSCVC4(STATE)

```

REAL*8 E1(0:100),E2(0:100),E3(0:100),E4(0:100),EVENT(0:500)
REAL*8 RS1(0:100),RS2(0:100),RS3(0:100),RS4(0:100),T,TEMP
REAL*8 TT(0:500,4),V
INTEGER CHANGE,CHECK,COUNT,IN,STATE,SUM
INTEGER TOTAL,TOT1,TOT2,TOT3,TOT4,X

```

```

OPEN(UNIT=41,FILE='STAT1.DAT',STATUS='OLD')
OPEN(UNIT=42,FILE='STAT2.DAT',STATUS='OLD')
OPEN(UNIT=43,FILE='STAT3.DAT',STATUS='OLD')
OPEN(UNIT=44,FILE='STAT4.DAT',STATUS='OLD')
OPEN(UNIT=60,FILE='TRACKER.DAT',STATUS='OLD')

```

```

REWIND(UNIT=60)

```

```

OPEN(UNIT=10,FILE='VIS1.DAT',STATUS='OLD')
OPEN(UNIT=11,FILE='VIS2.DAT',STATUS='OLD')
OPEN(UNIT=12,FILE='VIS3.DAT',STATUS='OLD')
OPEN(UNIT=13,FILE='VIS4.DAT',STATUS='OLD')
*****

```

```
DO 20 COUNT = 1,100
  READ(STATE,*END=25)E1(COUNT),RS1(COUNT)
  TOT1 = COUNT
20 CONTINUE
25 E1(0) = 0.0D0
```

```
IF (TOT1.EQ.0) THEN
  READ(10,*)T,V
  IF (V.GT.(0.0D0)) THEN
    RS1(0) = 1.0D0
  ELSE
    RS1(0) = 0.0D0
  ENDIF
ELSE IF (RS1(1).EQ.(0.0D0)) THEN
  RS1(0) = 1.0D0
ELSE
  RS1(0) = 0.0D0
ENDIF
```

```
*****  
* GROUND STATION AND SATELLITE #2 *  
*****
```

```
TOT2 = 0
DO 30 COUNT = 1,100
  READ(STATE+1,*END=35)E2(COUNT),RS2(COUNT)
  TOT2 = COUNT
30 CONTINUE
35 E2(0) = 0.0D0
```

```
IF (TOT2.EQ.0) THEN
  READ(11,*)T,V
  IF (V.GT.(0.0D0)) THEN
    RS2(0) = 1.0D0
  ELSE
    RS2(0) = 0.0D0
  ENDIF
ELSE IF (RS2(1).EQ.(0.0D0)) THEN
  RS2(0) = 1.0D0
ELSE
  RS2(0) = 0.0D0
ENDIF
```

```
*****  
* GROUND STATION AND SATELLITE #3 *  
*****
```

```
TOT3 = 0
DO 40 COUNT = 1,100
  READ(STATE+2,*END=45)E3(COUNT),RS3(COUNT)
  TOT3 = COUNT
40 CONTINUE
45 E3(0) = 0.0D0
```

```
IF (TOT3.EQ.0) THEN
  READ(12,*)T,V
  IF (V.GT.(0.0D0)) THEN
    RS3(0) = 1.0D0
  ELSE
    RS3(0) = 0.0D0
  ENDIF
ELSE IF (RS3(1).EQ.(0.0D0)) THEN
  RS3(0) = 1.0D0
ELSE
  RS3(0) = 0.0D0
ENDIF
```

```
*****
```

```

DO 50 COUNT = 1,100
READ(STATE+3,*,END=53)E4(COUNT),RS4(COUNT)
TOT4 = COUNT
50 CONTINUE
53 E4(0) = 0.0D0

IF (TOT4.EQ.0) THEN
READ(13,*)I,V
IF (V.GT.(0.0D0)) THEN
RS4(0) = 1.0D0
ELSE
RS4(0) = 0.0D0
ENDIF
ELSE IF (RS4(1).EQ.(0.0D0)) THEN
RS4(0) = 1.0D0
ELSE
RS4(0) = 0.0D0
ENDIF
*****
* The following calculates the total number of events between the *
* ground station and four satellites. *
*****
TOTAL = TOT1+TOT2+TOT3+TOT4
CHECK = 0
DO 55 COUNT = 1,500
READ(60,*,END=58)EVENT(COUNT)
CHECK = COUNT
55 CONTINUE
58 CONTINUE

IF (CHECK.EQ.0) THEN
WRITE(25,*)"There were no visibility opportunities with this
+ configuration."
GOTO 160
ENDIF
*****
* The following orders all the events from the smallest to the *
* largest. *
*****
DO 65 COUNT = 1,TOTAL-1
DO 60 X = 1,TOTAL-1
IF (EVENT(X+1).LT.EVENT(X)) THEN
TEMP = EVENT(X+1)
EVENT(X+1) = EVENT(X)
EVENT(X) = TEMP
ENDIF
60 CONTINUE
65 CONTINUE

EVENT(0) = 0.0D0

*****
* The following determines the status of communications for each *
* possible visibility path at each event. *
*****
DO 80 COUNT = 0,TOTAL
IF (TOT1.EQ.0) THEN
TT(COUNT,1) = RS1(0)
GOTO 80
ENDIF
DO 70 IN = 0,TOT1 - 1
IF (EVENT(COUNT).GE.E1(IN).AND.EVENT(COUNT).LT.E1(IN+1)) THEN
TT(COUNT,1) = RS1(IN)
GOTO 80

```

```
      GOTO 80
ELSE IF (EVENT(COUNT).GT.E1(IN+1).AND.IN.EQ.(TOT1-1)) THEN
    TT(COUNT,1) = RS1(IN+1)
    GOTO 80
ENDIF
70 CONTINUE
80 CONTINUE

DO 100 COUNT = 0,TOTAL
  IF (TOT2.EQ.0) THEN
    TT(COUNT,2) = RS2(0)
    GOTO 100
  ENDIF
DO 90 IN = 0,TOT2 - 1
  IF (EVENT(COUNT).GE.E2(IN).AND.EVENT(COUNT).LT.E2(IN+1)) THEN
    TT(COUNT,2) = RS2(IN)
    GOTO 100
  ELSE IF (EVENT(COUNT).EQ.E2(IN+1)) THEN
    TT(COUNT,2) = RS2(IN+1)
    GOTO 100
  ELSE IF (EVENT(COUNT).GT.E2(IN+1).AND.IN.EQ.(TOT2-1)) THEN
    TT(COUNT,2) = RS2(IN+1)
    GOTO 100
  ENDIF
90 CONTINUE
100 CONTINUE

DO 120 COUNT = 0,TOTAL
  IF (TOT3.EQ.0) THEN
    TT(COUNT,3) = RS3(0)
    GOTO 120
  ENDIF
DO 110 IN = 0,TOT3 - 1
  IF (EVENT(COUNT).GE.E3(IN).AND.EVENT(COUNT).LT.E3(IN+1)) THEN
    TT(COUNT,3) = RS3(IN)
    GOTO 120
  ELSE IF (EVENT(COUNT).EQ.E3(IN+1)) THEN
    TT(COUNT,3) = RS3(IN+1)
    GOTO 120
  ELSE IF (EVENT(COUNT).GT.E3(IN+1).AND.IN.EQ.(TOT3-1)) THEN
    TT(COUNT,3) = RS3(IN+1)
    GOTO 120
  ENDIF
110 CONTINUE
120 CONTINUE

DO 140 COUNT = 0,TOTAL
  IF (TOT4.EQ.0) THEN
    TT(COUNT,4) = RS4(0)
    GOTO 140
  ENDIF
DO 130 IN = 0,TOT4 - 1
  IF (EVENT(COUNT).GE.E4(IN).AND.EVENT(COUNT).LT.E4(IN+1)) THEN
    TT(COUNT,4) = RS4(IN)
    GOTO 140
  ELSE IF (EVENT(COUNT).EQ.E4(IN+1)) THEN
    TT(COUNT,4) = RS4(IN+1)
    GOTO 140
  ELSE IF (EVENT(COUNT).GT.E4(IN+1).AND.IN.EQ.(TOT4-1)) THEN
    TT(COUNT,4) = RS4(IN+1)
    GOTO 140
  ENDIF
130 CONTINUE
140 CONTINUE
```

```
*****
* The next DO loop determines if constant communication is      *
* possible. If the sum is equal to zero, communication is not    *
* possible. If the sum is greater than or equal to one, communica- *
* tion is possible.                                              *
*****
```

```
DO 150 COUNT = 0,TOTAL
SUM = TT(COUNT,1) + TT(COUNT,2) + TT(COUNT,3) + TT(COUNT,4)
IF (SUM.EQ.(0.0D0).AND.CHANGE.EQ.1) THEN
  WRITE(25,*)'Communications broken at ',EVENT(COUNT)
  CHANGE = 0
ENDIF

IF (SUM.GE.(1.0D0).AND.CHANGE.EQ.0) THEN
  WRITE(25,*)'Communications re-established at ',EVENT(COUNT)
  CHANGE = 1
ENDIF

150 CONTINUE
160 CONTINUE

CLOSE(UNIT=STATE,STATUS='DELETE')
CLOSE(UNIT=STATE+1,STATUS='DELETE')
CLOSE(UNIT=STATE+2,STATUS='DELETE')
CLOSE(UNIT=STATE+3,STATUS='DELETE')
CLOSE(UNIT=60)
CLOSE(UNIT=10,STATUS='DELETE')
CLOSE(UNIT=11,STATUS='DELETE')
CLOSE(UNIT=12,STATUS='DELETE')
CLOSE(UNIT=13,STATUS='DELETE')

RETURN

END
```

**END**

**FILMED**

DATE:

**1-92**

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